

# Global Value Chains and Inequality with Endogenous Labor Supply

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<sup>1</sup>The views expressed here are those of the authors and are not necessarily reflective of views of the Federal Reserve Banks of Dallas, Minneapolis, or the Federal Reserve System.

# Motivation

- Key feature of increased international trade is increased prevalence of global value chains (GVCs)
  - ▶ Value-added exports as share of total exports fell 10 percentage points between 1970 and 2009 (Johnson and Noguera, 2016)
  - ▶ GVC generates magnified effects of trade costs and decline in trade costs on trade flows (e.g., Yi, 2003, 2010)
- Much research has shown that increased international trade has increased inequality
  - ▶ Goldberg and Pavcnik (2007) survey suggests that more countries experience increase in inequality than implied by Heckscher-Ohlin model and Stolper-Samuelson implications
- What is role of GVCs in increased inequality?

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# This Paper

- What We Do

- ① Develop **multi-sector model of GVCs with endogenous occupational choice**

- ★ Two GVC mechanisms: “roundabout” and “snake”

- ★ Roy mechanism: Facilitates general sorting pattern among workers

- ② Quantitatively assess role of GVCs in propagating globalization shocks on aggregate and distributional outcomes within and across countries

- In response to decline in China’s trade costs, calibrated model implies:

- ▶ Increase in skill premium in both China and the U.S.

- ★ GVCs lead to increased specialization across stages, which leads to skill upgrading in both countries

- ▶ GVCs magnify aggregate and increase distributional outcomes in China and U.S.

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# Related Research

- Aggregate effects of **vertical specialization**

- ▶ Documentation and models: Hummels et al. (2001), Yi (2003;2010), Johnson and Noguera (2012; 2016), Antras et al. (2013), Fally and Hillberry (2014), Johnson and Moxnes (2015)
- ▶ Recently: **Antras and de Gortari (2017)**, **de Gortari (2017)**

- **Roy-like assignment framework**

- ▶ Theory: Costinot and Vogel (2010)
- ▶ Quantitative approach: Lagakos and Waugh (2013), Hsieh et al. (2016), Burstein et al. (2016), **Lee (2017)**, Galle et al. (2017)

- Sectoral linkage of production: Caliendo and Parro (2015)

- Offshoring and the skill premium: Feenstra and Hanson (1996), Zhu and Treffler (2005), Krugman (2008), Costinot and Vogel (2010)

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# Outline

- 1 Introduction
- 2  $2^5$  Version of Model
- 3 Numerical Exercises with  $2^5$  Model
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# Basic Setup

- 2 countries ( $i = 1, 2$ : source;  $n = 1, 2$ : destination)
- 2 sectors ( $s = 1, 2$ )
- 2 occupations ( $o = L, H$ )
- 2 stages of production ( $j = 1, 2$ )
- 2 worker types ( $t = L, H$ )

Goods market: Comparative advantage determines which goods and stages are made in which source country and are shipped to which destination country

Labor market: Firms' occupational demands interact with workers' occupational supply (Roy model)

# Preferences

- Nested preferences
  - ▶ Cobb-Douglas preferences across sectors with expenditure share  $b^s \in [0, 1]$
  - ▶ CES preferences over products within sector with elasticity of substitution  $\sigma > 0$

# Production Functions

There is a continuum of goods  $\omega$  on the unit interval in each sector

- Production function for each stage:

$$f_i^{s,1}(\omega) = z_i^{s,1}(\omega)(x_i^{s,1})^{1-\alpha_i^s}((L_i^{s,1,H}(\omega))^{\beta^{1,H}}(L_i^{s,1,L}(\omega))^{\beta^{1,L}})^{\alpha_i^s}$$

$$f_i^{s,2}(\omega) = z_i^{s,2}(\omega)[(x_i^{s,2})^{1-\alpha_i^s}((L_i^{s,2,H}(\omega))^{\beta^{2,H}}(L_i^{s,2,L}(\omega))^{\beta^{2,L}})^{\alpha_i^s}]^{\gamma^s}(m_i^{s,1}(\omega))^{1-\gamma^s}$$

- $z_i^{s,j}$ : Fréchet productivity parameter
- $x_i^{s,j}$ : Composite intermediate used in production ("roundabout")
- $L_i^{s,j,o}$ : Occupational input  $o$  used in production
- $m_i^{s,1}$ : Stage 1-good used in stage-2 production ("snake")
- $1 - \gamma^s \in [0, 1]$ : share of stage-1 good in stage-2 production
- $\alpha_i^s \in [0, 1]$ : value-added share (1-composite intermediate share)
- $\beta^{j,o} \in [0, 1]$ : occupation intensity for occupation  $o$ 
  - ▶  $\beta^{j,H} + \beta^{j,L} = 1$  for every  $j$

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# Sourcing Problem

- Perfect competition
- Stage 2 producers buy stage 1 materials from home or abroad, and composite intermediate “aggregator” firms buy stage 2 goods from home or abroad
- Iceberg trade costs:  $\tau_{in}^s \geq 1$
- Productivity draws as in Eaton and Kortum (2002) and Antras and de Gortari (2017)

$$z_i^{s,j}(\omega) \sim F_i^{s,j}(z) = \exp(-A_i^s z^{-\nu} \tilde{\gamma}^{s,j}),$$

where  $\tilde{\gamma}^{s,1} \equiv 1 - \gamma^s$  and  $\tilde{\gamma}^{s,2} \equiv 1$

- We draw from decentralized approach of Antras and de Gortari (2017)
  - ▶ Independent sourcing
  - ▶ Limited information on upstream productivities
- Composite sectoral good is consumed, or aggregated with other composite sectoral goods to form an overall composite intermediate, which is used in stage-1 and stage-2 production (roundabout channel)

Sourcing Equilibrium



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Sourcing Equilibrium

# Heterogeneous Workers

- Type-level labor supply  $\bar{L}_{i,t}$  is exogenously given
- Within each type, workers are heterogeneous in (sector, occupation)-specific productivities
  - ▶  $\Rightarrow$  “Roy” mechanism

- $\epsilon^{s,o}$ : Idiosyncratic productivity of individual worker for  $(s, o)$ 
  - ▶ Randomly drawn from a Fréchet distribution:

$$G_t^{s,o}(\epsilon) = \exp(-T_t^{s,o} \epsilon^{-\theta_t})$$

- ▶ Interpretation: efficiency units of labor
- ▶  $\theta_\tau$ : Within-type dispersion of productivity, **labor supply elasticity**
- ▶  $T_t^{s,o}$ : Level of labor productivity

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# Equilibrium Labor Supply and Wages

- Worker's problem characterizes the Roy mechanism:

$$\max_{s,o} w_i^{s,o} \epsilon^{s,o}$$

- Equilibrium labor supply:

$$\pi_{i,t}^{s,o} = \frac{T_t^{s,o} (w_i^{s,o})^{\theta_t}}{\sum_{s',o'} T_t^{s',o'} (w_i^{s',o'})^{\theta_t}}$$

- Equilibrium type-level average wage:

$$\bar{w}_{i,t} = \left[ \sum_{s',o'} T_t^{s',o'} (w_i^{s',o'})^{\theta_t} \right]^{1/\theta_t} \Gamma(1 - \frac{1}{\theta_t})$$

- Skill premium: ratio of  $\bar{w}_{i,H}$  to  $\bar{w}_{i,L}$

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## 2<sup>5</sup> Model: Equilibrium

- Equilibrium probability of a GVC path  $l = (l^1, l^2)$

Details

$$\lambda_{l,i}^s = \frac{A_{l^1}^s (c_{l^1}^{s,1} \tau_{l^1 l^2}^s)^{-\nu(1-\gamma^s)} \times A_{l^2}^s [(c_{l^2}^{s,2})^{\gamma^s} \tau_{l^2 i}^s]^{-\nu}}{\sum_{l' \in \mathbf{N}^2} A_{l'^1}^s (c_{l'^1}^{s,1} \tau_{l'^1 l'^2}^s)^{-\nu(1-\gamma^s)} \times A_{l'^2}^s [(c_{l'^2}^{s,2})^{\gamma^s} \tau_{l'^2 i}^s]^{-\nu}}$$

- Effect of changes in trade costs on aggregate trade flows can be multiplied

- Labor market clearing:

$$\frac{1}{\alpha_i^s} \sum_t \bar{w}_{i,t} \pi_{i,t}^{s,o} \bar{L}_{i,t} = \underbrace{(1-\gamma^s) \beta^{1,o} \sum_{n=1}^N \sum_{l \in \Lambda_i^1} \lambda_{l,n}^s X_n^s}_{\text{stage 1's contribution}} + \underbrace{\gamma^s \beta^{2,o} \sum_{n=1}^N \sum_{l \in \Lambda_i^2} \lambda_{l,n}^s X_n^s}_{\text{stage 2's contribution}}$$

where  $X_n^s \equiv b^s [\sum_t \bar{w}_{n,t} \bar{L}_{n,t} + \sum_{s'} \frac{(1-\alpha_{n'}^{s'})}{\alpha_{n'}^{s'}} \sum_o \sum_t \bar{w}_{n,t} \pi_{n,t}^{s',o} \bar{L}_{n,t}]$

- Extreme GVC intensities imply stage specialization is irrelevant for skill premium

General Version

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General Version

# Transmission channels

- Four main channels:
  - ① Country-level comparative advantage: HO and Ricardian
  - ② “Roundabout” production structure
  - ③ “Snake” production structure  $\Rightarrow$  global value chain (GVC)
  - ④ Worker-level comparative advantage: “Roy” channel
- Our model builds bridges between these channels

# Interaction of Comparative Advantages and Skill Premia

- HO comparative advantage
  - ▶ Across **production stages** via relative endowments of labor and  $\beta^{j,o}$ .
  - ▶ Across **sectors** if  $1 - \alpha^s$  or  $1 - \gamma^s$  vary across sectors
- Ricardian comparative advantage (CA)
  - ▶ Across **sectors** via relative  $A_i^s$  in conjunction with Roy worker sorting into CA sector and the occupation for which workers have relatively high productivity
    - ★  $1 - \gamma^s$  plays a role, because it determines how much sector specialization feeds into demand for occupations
- Roy (worker-level) comparative advantage
  - ▶ Across **sectors** and **occupations**: based on  $T_i^{s,o}$

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## 2<sup>5</sup> Model: Numerical Example

- Focus on how HO and the Roy mechanisms operate through GVC
- We set parameter values so that **country 1** has a HO comparative advantage in **stage 1** and **sector 1**
  - ▶ Stage 1 uses **low-skilled occupations** more intensively
- Two counterfactual trade costs:  $\tau_{in}^s = 2$  and  $\tau_{in}^s = 1$  for all  $i, n$ , and  $s$
- Results (when trade costs fall)
  - ▶ Aggregate effect: **greater specialization in stages of production**
    - ★ Domestic sourcing becomes less likely (e.g., falls from 83.7% to 26.4% in sector 1)
    - ★ Most prevalent GVC is  $I = (1, 2)$
  - ▶ Skill premium ( $\bar{w}_{i,H}/\bar{w}_{i,L}$ ) decreases (-1.11%) in country 1 and increases (+1.08%) in country 2
    - ★ Stolper-Samuelson effects
- Workers switch sectors AND occupations

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    - ★ Most prevalent GVC is  $I = (1, 2)$
  - ▶ Skill premium ( $\bar{w}_{i,H}/\bar{w}_{i,L}$ ) **decreases (-1.11%) in country 1** and **increases (+1.08%) in country 2**
    - ★ Stolper-Samuelson effects
- Workers switch sectors AND occupations

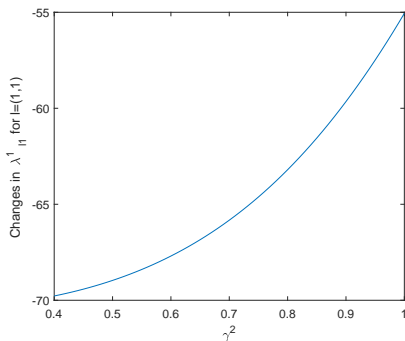
## 2<sup>5</sup> Model: GVC Intensity and Domestic Sourcing

- **GVC magnifies effect of decline in trade costs on trade flows**

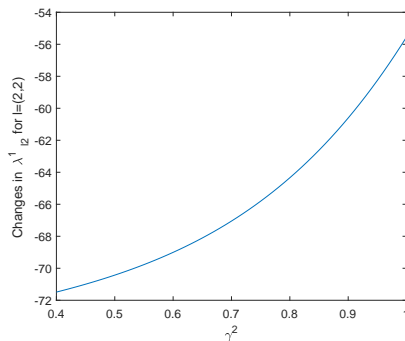
- Exercise:

- ▶ keep  $\gamma^1 - \gamma^2 < 0$  fixed; raise or lower  $\gamma^1$  (and  $\gamma^2$ )
- ▶ Plot changes in domestic sourcing probability  $\lambda_{(i,i),i}^s$

(a) Country 1, sector 1



(b) Country 2, sector 1

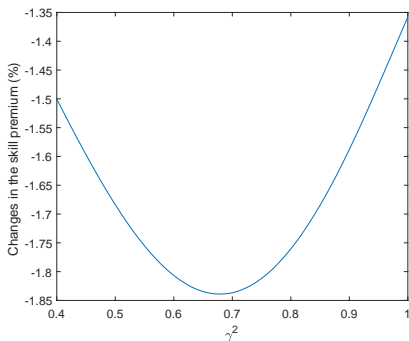


- Larger magnification effects with lower  $\gamma^s$ ; monotonic magnification effects

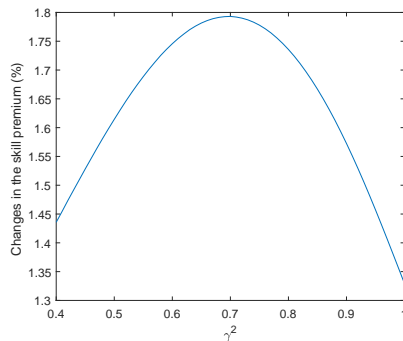
## 2<sup>5</sup> Model: GVC Intensity and the Skill Premium

- **Non-monotonic effects of the GVC intensity on the skill premium**

(a) Country 1



(b) Country 2



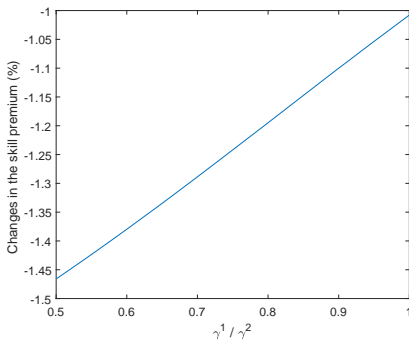
- With extreme GVC intensities, skill premium affected only by sector specialization – therefore, smaller changes

## 2<sup>5</sup> Model: Sectoral Variation in GVC Intensity

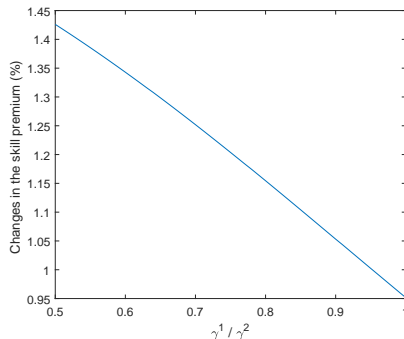
Exercise:

- Move  $\gamma^1$  and  $\gamma^2$  in opposite directions in order to reinforce HO CA
  - ▶ Make stage 1 (stage 2) more important for sector 1 (sector 2)
  - ▶ Implies that each country's CA (stage,sector) becomes more important
- Plot changes in the skill premium from decline in trade costs

(a) Country 1



(b) Country 2



**Larger skill premium effects if higher weights on CA stage and CA sector**

# Outline

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- 2  $2^5$  Version of Model
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# Roadmap

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3 Countries	China, US, ROW
5 Worker Types	Based on Education
4 Sectors	Agr, Min, Mfg, Svc
2 Production stages	Stage 1, stage 2
5 Occupations	Based on required skill level

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- Data: WIOD 2000 and ACS 2000

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- Data: WIOD 2000 and ACS 2000
- Parameters
  - ▶ Assigned:  $\sigma$  (2) and  $\nu$  (4)
  - ▶ Calibrated from data:  $b^s$ ,  $\bar{L}_{i,t}$ , and  $\tau_{in}^s$
  - ▶ Estimated from data:  $T_t^{s,o}$  and  $\theta_t$  (Roy parameters)
  - ▶ Calibrated by matching moments of model:  $A_i^s$ ,  $\gamma^{s,j}$ ,  $\alpha_i^s$ , and  $\beta_i^{j,o}$

# Calibration of Bilateral Trade Costs

- Use WIOD IO tables for data counterpart of bilateral final goods trade flows:

$$\tilde{\lambda}_{in}^{F,s} = \sum_{l \in \Lambda_i^J} \lambda_{l,n}^s$$

- Assume symmetry of bilateral trade costs, then use Head-Ries index to back out  $\tau_{in}^s$  conditional on  $\nu$

# Estimation of Roy Parameters

- Assume that Roy parameters ( $T_t^{s,o}$  and  $\theta_t$ ) do not vary by country
  - ▶ Parameters govern complementarity between skill and (sector,occupation)-specific task
- Use within-type wage distribution in U.S. in 2000 to jointly estimate  $\sum_{s,o} T_t^{s,o} (w_{US}^{s,o})^{\theta_t}$  and  $\theta_t$  for each type  $t$  using MLE
- Use  $\pi_{US,t}^{s,o}$  in 2000 to back out  $T_t^{s,o}$  up to normalization (cf. Hsieh et al. (2013))
- Results
  - ▶ More within-type heterogeneity for higher skilled workers
  - ▶ Better educated workers have CA in the service sector and high-skilled occupations

Graph on T

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# Main Calibration

- Need to calibrate:
  - ▶  $\gamma^s$ : share of stage 2 value-added (1— GVC intensity)
  - ▶  $\alpha_i^s$ : value-added share
  - ▶  $A_i^s$ : sector- and country-level average productivity level
  - ▶  $\beta_i^{j,o}$ : occupation intensity in each stage and each country
- Calibrate by targeting moments:
  - ▶ Domestic absorption of final/intermediate goods for each sector and each country
  - ▶ Ratio of value added to gross output for each sector and each country
  - ▶ Share of each country's GDP in each sector
  - ▶ Share of labor payment to each occupation group in each sector in each country
- Conditional on parameters already calibrated/estimated:  $\nu$ ,  $\sigma$ ,  $b^s$ ,  $\bar{L}_{i,t}$ ,  $\theta_t$ ,  $T_t^{s,o}$ , and  $\tau_{in}^s$



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# Main Calibration: Results

- $\beta_i^{j,o}$ : Occupation intensities vary a lot by stage and country. For example,

Stage 1		Stage 2
US	high-skilled o intensive	low-skilled o intensive
China	low-skilled o intensive	high-skilled o intensive

- $\gamma^s$ : GVC intensities vary by sector
  - ▶ Relatively lower in agriculture (0.12) and manufacturing (0.39)
  - ▶ Relatively higher in mining (0.50) and services (0.44)
- $\alpha_i^s$ : also varies significantly by country and sector (avg 0.50; std dev 0.22)
- $A_i^s$ : China (US) has a Ricardian comparative advantage in manufacturing (in service)

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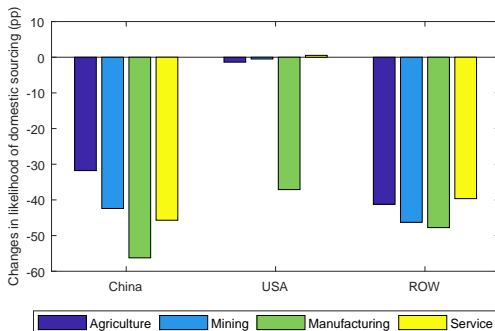
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- Changes in prevalence of domestic sourcing:  $\lambda_{(i,i),i}^s$ 
  - ▶ Domestic sourcing becomes less likely everywhere



# Specialization and the Skill Premium

- **Sector specialization:** US specializes in services, China specializes in manufacturing
  - ▶ Through Roy channel, higher educated workers have CA in services
  - ▶ Leads to **increase (decrease)** in skill premium **in the U.S. (in China)**
- **Stage specialization:** Three key outcomes drive results.
  - ① Within sectors, US specializes in stage 1, China specializes in stage 2
  - ② Stage 1 (stage 2) is more high-skilled-occupation-intensive in the U.S. (in China); hence, both countries specialize in high-skilled-occupation-intensive stage
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Graph

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Graph



# Distributional Effect of China Shock

- Changes in the skill premium:  $\bar{w}_{i,H}/\bar{w}_{i,L}$

	China	USA	ROW
% Baseline	0.25	0.94	1.09
% No GVC (no recalib)	-1.16	0.17	1.04
% No GVC (recalib)	-0.39	0.02	0.50

- The GVC channel is more important than sector specialization
- U.S. has CA in, and specializes in, **stage 1** and **service** sector
  - Both sector and stage specializations increase U.S. skill premium
- China has CA in, and specializes in **stage 2** and **manufacturing** sector
  - Low-skilled workers have CA in **manufacturing**, which leads to **lower** skill premium
  - Stage 2** is relatively high-skilled-occupation-intensive in China
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# Alternative Counterfactuals

- Two alternative counterfactuals
- Alternative 1: Shut down the GVC channel by setting  $\gamma^s = 1$ . Do not recalibrate other parameters.
  - ▶ Only sector specialization affects the skill premium
  - ▶ The skill premium **increases** in the **U.S.** by **0.17%**
  - ▶ The skill premium **decreases** in **China** by **1.16%**
- Alternative 2: Fix  $\beta_i^{j,o}$ ; set  $\gamma^{MFG} = 1$  and  $\gamma^{SVC} = 0$ 
  - ▶ Puts the maximum weights on each country's CA (stage,sector)
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GVC channel:

- **Magnifies aggregate** effects of China trade shock
- **Delivers skill upgrading story** through stage specialization
  - ▶ Direction of changes in the skill premium
- **Increases distributional effects of the China trade shock**, but, because of lower weights on each country's CA (stage,sector)
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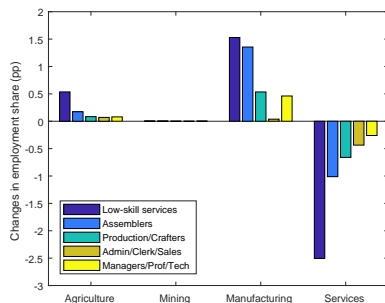
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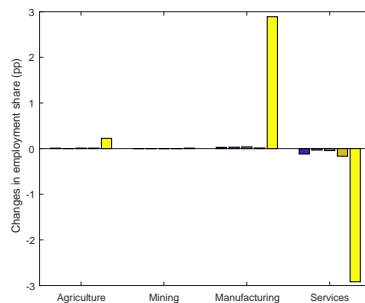
# Within-type Labor Reallocation

- Different labor reallocation patterns across different worker types
- For example, in China,

(a) High school dropouts



(b) Advanced degrees



USA

# Conclusion

- Develop multi-sector GVC model with endogenous labor supply that builds bridges between country-level CA, worker-level CA, and two types of GVCs (snake and roundabout)
- Quantitatively assess the role of GVCs in transmitting trade shocks to aggregate and distributional outcomes
- Quantitative results suggest that:
  - ▶ GVCs magnify aggregate effects, and increase distributional effects, of trade liberalization on China and U.S.
  - ▶ A skill upgrading story can occur via the GVC channel
  - ▶ Effect of GVC (stage specialization) on the skill premium is larger than that of sector specialization
  - ▶ Sectoral variation in GVC intensity is important in determining magnitude of effect

# Multi-stage Production

- Production function:

$$f_i^{s,j}(x_i^{s,j}, L_i^{s,j,1}(\omega), \dots, L_i^{s,j,O}(\omega), m_i^{s,j-1}(\omega)) =$$

$$z_i^{s,j}(\omega) ((x_i^{s,j})^{1-\alpha_i^s} \prod_o (L_i^{s,j,o}(\omega))^{\beta_i^{j,o} \alpha_i^s})^{\gamma^{s,j}} (m_i^{s,j-1}(\omega))^{1-\gamma^{s,j}}$$

- $(1 - \gamma^{s,j}) \in [0, 1]$ : share of stage  $(j - 1)$  materials in stage  $j$  production
  - ▶ GVC intensity
  - ▶ Note  $\gamma^{s,1} \equiv 1$  for every  $s$
- $\alpha_i^s \in [0, 1]$ : value-added share
- $\beta_i^{j,o} \in [0, 1]$ : occupation intensity at stage  $j$  in country  $i$ 
  - ▶  $\sum_o \beta_i^{j,o} = 1$  for every  $i$  and  $j$

# Sourcing Decision: Equilibrium

- Probability of the entire GVC path

$$\lambda_{l,i}^s = \frac{\prod_{j=1}^J A_{lj}^{s,j} [(c_{lj}^{s,j})^{\gamma^{s,j}} (\tau_{lj|j+1}^s)]^{-\nu \tilde{\gamma}^{s,j}}}{\sum_{l' \in \mathbf{N}^J} \prod_{j=1}^J A_{l'j}^{s,j} [(c_{l'j}^{s,j})^{\gamma^{s,j}} (\tau_{l'j|j+1}^s)]^{-\nu \tilde{\gamma}^{s,j}}}$$

where  $\mathbf{N}^J$  is a set of all  $J$ -dim permutations of  $N$  countries

- Overall effective trade elasticity is larger if GVC intensity is larger
- Effective trade elasticity is larger in downstream stages

[Unit cost equation](#)

[Exact price index](#)

[Sourcing Problem: Detail](#)

[Back:Main](#)

# Unit Cost and Price Index

- Unit cost of input bundle excluding stage  $j - 1$  materials

$$c_i^{s,j} \equiv \varphi_i^{s,j} (P_i)^{1-\alpha_i^s} \prod_o (w_i^{s,o})^{\alpha_i^s \beta_i^{j,o}}$$

for some constant  $\varphi_i^{s,j}$

- Sector-level exact price index

$$P_i^s = [\Gamma(\frac{\nu + 1 - \sigma}{\nu})]^{1/(1-\sigma)} (\sum_{l' \in \mathbf{N}^J} \prod_{j=1}^J A_{l'j}^{s,j} [(c_{l'j}^{s,j})^{\gamma^{s,j}} (\tau_{l'j|l'j+1}^s)]^{-\nu \tilde{\gamma}^{s,j}})^{-1/\nu}$$

Back:Sourcing1

# Sourcing Equilibrium: Details

- Stage 1:

$$l_i^{s,1}(\omega) = \arg \min_l [(p_l^{s,1}(\omega) \tau_{li}^s)^{1-\gamma^{s,2}}] = \arg \min_l [(\frac{c_l^{s,1}}{z_l^{s,1}(\omega)} \tau_{li}^s)^{1-\gamma^{s,2}}]$$

- Stage  $j$ :

$$l_i^{s,j}(\omega) = \arg \min_l \{ (\frac{c_l^{s,j}}{z_l^{s,j}(\omega)})^{\gamma^{s,j}} \}^{1-\gamma^{s,j+1}} \times \Theta_l^{s,j-1}((1-\gamma^{s,j+1})(1-\gamma^{s,j})) \times (\tau_{li}^s)^{1-\gamma^{s,j+1}} \}$$

where  $\Theta_i^{s,j}(x) \equiv E_j[(p_{l_i^{s,j}(\omega)}^{s,j}(\omega) \tau_{l_i^{s,j}(\omega)i}^s)^x]$

- Equilibrium probability of stage  $j$  sourcing

$$\Pr(l_i^{s,j}(\omega) = n) = \frac{A_n^{s,j}(B_{ni}^{s,j})^{-\nu \tilde{\gamma}^{s,j}/(1-\gamma^{s,j+1})}}{\sum_{n'} A_{n'}^{s,j}(B_{n'i}^{s,j})^{-\nu \tilde{\gamma}^{s,j}/(1-\gamma^{s,j+1})}}$$

where  $B_{ni}^{s,j} \equiv (c_n^{s,j})^{\gamma^{s,j}(1-\gamma^{s,j+1})} \times \Theta_n^{s,j-1}((1-\gamma^{s,j+1})(1-\gamma^{s,j})) \times (\tau_{ni}^s)^{1-\gamma^{s,j+1}}$

# Details of the Simple 2<sup>s</sup> Case

- Production function for each stage:

$$z_i^{s,1}(\omega)(x_i^{s,1})^{1-\alpha_i^s}((L_i^{s,1,H}(\omega))^{\beta^{1,H}}(L_i^{s,1,L}(\omega))^{\beta^{1,L}})^{\alpha_i^s}$$

$$z_i^2(\omega)[(x_i^{s,2})^{1-\alpha_i^s}((L_i^{s,2,H}(\omega))^{\beta^{2,H}}(L_i^{s,2,L}(\omega))^{\beta^{2,L}})^{\alpha_i^s}]^{\gamma^s}(m_i^{s,1}(\omega))^{1-\gamma^s}$$

- Stage 1 sourcing decision:

$$l_i^{s,1}(\omega) = \arg \min_l [(p_l^{s,1}(\omega)\tau_{li}^s)^{1-\gamma^s}] = \arg \min_l [(\frac{c_l^{s,1}}{z_l^{s,1}(\omega)}\tau_{li}^s)^{1-\gamma^s}]$$

- Stage 2 sourcing decision:

$$l_i^{s,2}(\omega) = \arg \min_l [\frac{(c_l^{s,2})^{\gamma^s}}{z_l^{s,2}(\omega)} \times \Theta_l^s \times \tau_{li}^s]$$

Back: Equilibrium of the simple version

# Labor Market Clearing Conditions

- Equilibrium  $w_i^{s,o}$  solves the following set of  $(N \times S \times O)$  labor market clearing conditions

$$\underbrace{\frac{1}{\alpha_i^s} \sum_t \bar{w}_{i,t} \pi_{i,t}^{s,o} \bar{L}_{i,t}}_{\text{labor supply}} = \underbrace{\sum_j \gamma^{s,j} \tilde{\gamma}^{s,j} \beta_i^{j,o} \sum_{n=1}^N \sum_{l \in \Lambda_i^j} \lambda_{l,n}^s X_n^s}_{\text{labor demand}}$$

$$X_n^s \equiv b^s \left[ \sum_t \bar{w}_{n,t} \bar{L}_{n,t} + \sum_{s'} \frac{(1 - \alpha_n^{s'})}{\alpha_n^{s'}} \sum_o \sum_t \bar{w}_{n,t} \pi_{n,t}^{s',o} \bar{L}_{n,t} \right]$$

where  $\Lambda_i^j \equiv \{l = (l^1, \dots, l^J) \in \mathbf{N}^J \mid l^j = i\}$ , up to a normalization

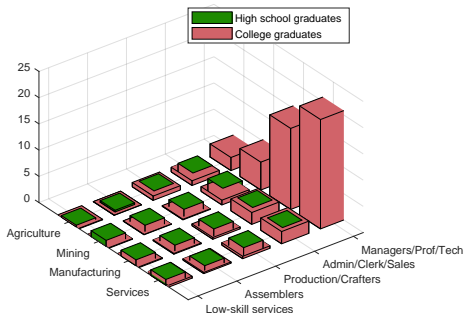
Back : 2<sup>5</sup> case



# Estimation of the Roy Parameters: Result

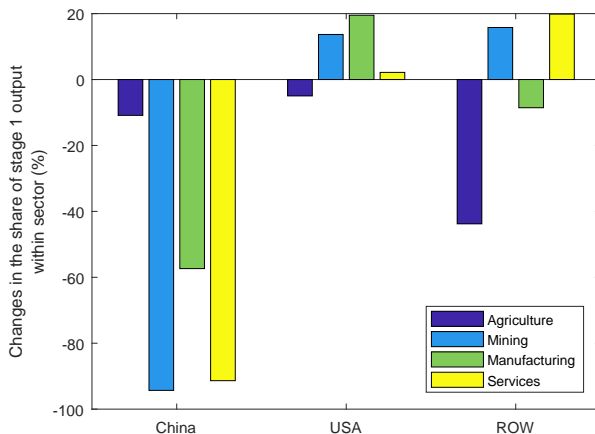
Worker type	$t_1$	$t_2$	$t_3$	$t_4$	$t_5$
Estimated $\theta_t$	1.97	1.86	1.74	1.60	1.48

- Compare the estimates of  $T_t^{s,o}$  for



# Aggregate Effect of China Shock: Specialization

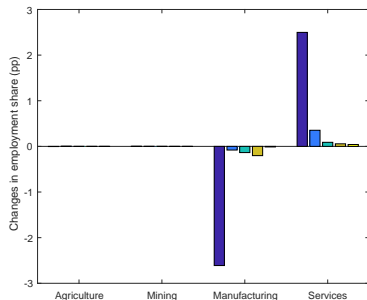
- Changes in the share of stage 1 output within each sector



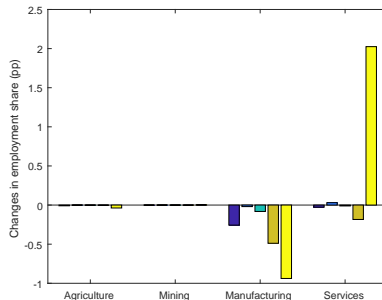
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- Different labor reallocation patterns across different worker types
- For example, in the US,

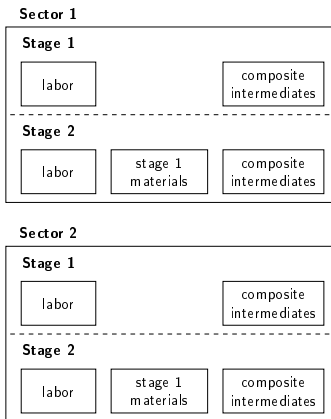
(a) High school dropouts



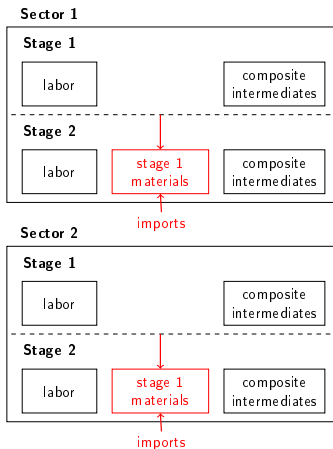
(b) Advanced degrees



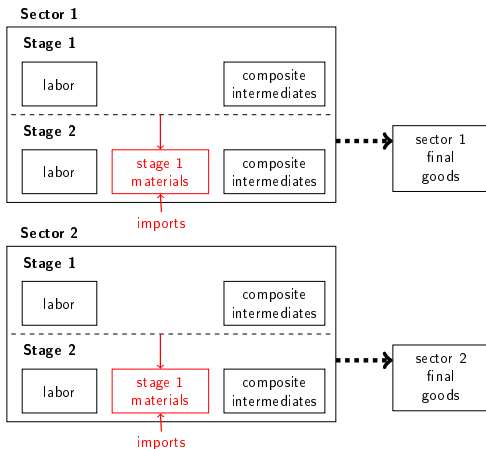
# Graphical Illustration of the Model: Production



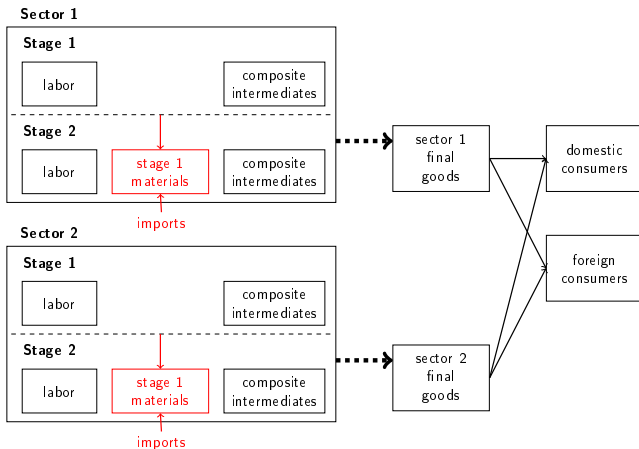
# Graphical Illustration of the Model: Production



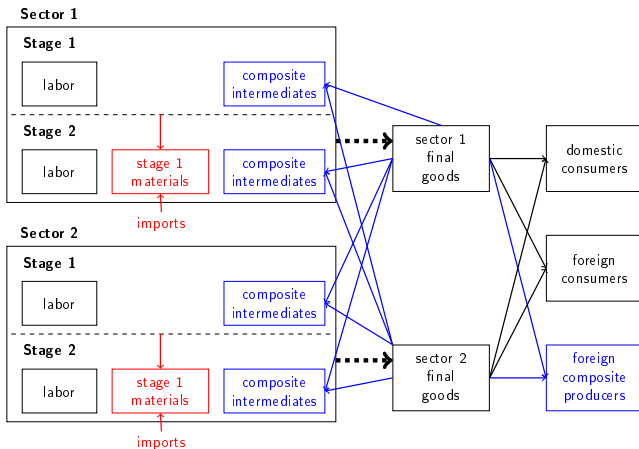
# Graphical Illustration of the Model: Production



# Graphical Illustration of the Model: Production

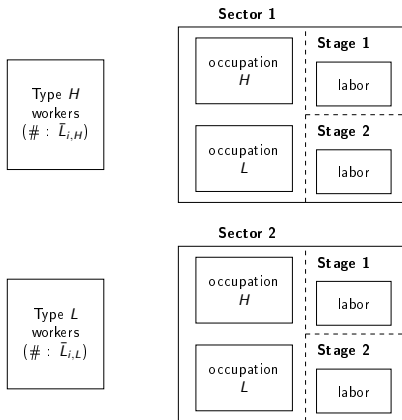


# Graphical Illustration of the Model: Production

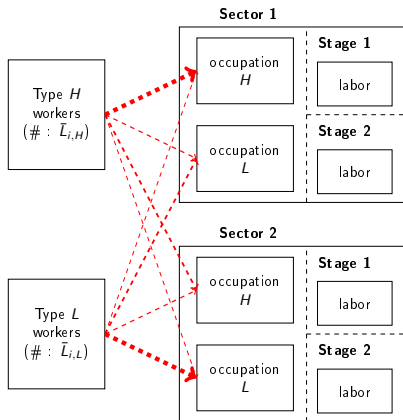




# Graphical Illustration of the Model: Workers



# Graphical Illustration of the Model: Workers



# Graphical Illustration of the Model: Workers

