

Efficient Recapitalization ^{*}

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Abstract

We analyze public interventions to alleviate debt overhang among private firms when the government has limited information and limited resources. We compare the efficiency of buying equity, purchasing existing assets, and providing debt guarantees. With symmetric information, all the interventions are equivalent. With asymmetric information between firms and the government, buying equity dominates the two other interventions. We solve for the optimal intervention, and show how it can be implemented with subordinated loans and warrants.

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It is well understood since the seminal work of Myers (1977) that debt overhang can lead to under-investment. Firms in financial distress find it difficult to raise capital for new investments because the proceeds from these new investments mostly serve to increase the value of the existing debt instead of equity.

A theoretical solution to debt overhang is renegotiation between equity and debt holders. If renegotiation is costless, efficiency is restored. In practice, however, renegotiation often requires bankruptcy, which is a costly process. Indeed, a large body of empirical research has shown the economic importance of private renegotiation costs for firms in financial distress (see Gilson, John, and Lang (1990), Asquith, Gertner, and Scharfstein (1994), Hennessy (2004) among others). The social costs of renegotiation may be even larger than the private costs because renegotiations can trigger creditor runs among other firms. Moreover, from a theoretical perspective, one should expect renegotiation to be costly because otherwise debt would not discipline managers or reduce risk shifting (Hart and Moore (1995), Jensen and Meckling (1976)). Hence, debt holders are often dispersed which makes it difficult to renegotiate outside bankruptcy because of free-rider problems or contract incompleteness (see Bulow and Shoven (1978), Gertner and Scharfstein (1991), and Bhattacharya and Faure-Grimaud (2001)).

If the deadweight losses from debt overhang and bankruptcy are high, there might be room for an intervention by the government. The government can alleviate the debt overhang problem by providing capital to firms directly. However, if the government intervenes, this raises the question of how to intervene efficiently.

The goal of our paper is analyze the optimal form of government intervention in a standard model of debt overhang. In our model firms differ across two dimensions. The first dimension is the quality of their investment opportunities. If the quality of investment opportunities is high, there is a welfare loss from not investing. The second dimension is the quality of assets in place. If asset quality is low, debt overhang is severe and firms under-invest. The information structure is such that, under symmetric information, the government and firms only know the distribution of future investment opportunities and asset values. Under asymmetric information, firms know the asset values and investment opportunities of each firm but the government does not.

We compare three different interventions. The first intervention is to purchase an equity

stake in the firm. The second intervention is to buy a share of the firm's assets. The third intervention is to provide debt guarantees to the firm. We also consider combinations of the three interventions and solve for the optimal intervention. The government's objective is to trade off the benefits from reducing debt overhang and the expected cost of the intervention.

All government interventions under consideration alter the firm's balance sheet and thus change the firm's incentives to invest under debt overhang. As a result, government interventions create different payoff structures for the government, the equity holders, and the debt holders. It is therefore far from obvious which intervention is more efficient. In fact, it is not even clear that there exists a ranking of interventions in terms of efficiency.

Our analysis of interventions delivers two results. The first result is that, if firms and the government have the same information at the time that firms decide whether to participate in a government program, all interventions are equivalent. The intuition for this result comes in three steps. First, if firms and the government have the same information, the firm's participation constraint is the same under all programs. The government then extracts the expected payoff from future investment opportunities by keeping equity holders to their reservation utility. Second, all interventions reduce debt overhang to the same extent as long as the interventions provide the same amount of financing. Third, the cost to the government is the implicit transfer to debt holders minus the expected gain from future investment opportunities. This cost is the same across all interventions as long as the government provides the same amount of financing and extracts all surplus from equity holders.

The second result is that, if firms have better information than the government at the time that firms decide whether to participate in a government program, buying equity dominates the two other interventions. The intuition for this result also comes in three steps. First, under asymmetric information firms participate in interventions based on private information about asset quality and investment opportunities. Hence, participating firms receive informational rents. Second, since all interventions are equivalent under symmetric information, the ranking of government interventions under asymmetric information has to come from better selection and lower rents of participating firms. Third, under asymmetric information there are many firms that opportunistically participate in a government program even though they would invest without the program. Buying equity reduces oppor-

tunistic participation more than other interventions because buying equity provides a share in the firm's assets *and* investment opportunities, while other interventions only provide a share in the firm's assets. As a result, firms with good assets and good investment opportunities are less likely to participate opportunistically under the equity program relative to other programs.

Our results on symmetric versus asymmetric information also shed light on the comparison between compulsory and voluntary interventions. The symmetric information case is equivalent to compulsory participation under the constraint that the intervention is *acceptable for the average firm*. With voluntary participation, firms select to participate based on the value of assets in place and their investment opportunities. The endogenous selection can be costly because firms with assets of lower quality are more likely to participate, but it can also be beneficial because firms with good investment opportunities are more likely to participate. We can show that compulsory interventions dominate voluntary ones when the intervention is large.

We then solve for the optimal intervention where the government provides a subordinated loan (or buys preferred stock) in exchange for warrants. The loan is subordinated because the government does not want to generate additional debt overhang. The government asks for warrants because this allows the government to extract the entire surplus from future investment opportunities. We show that this intervention is equivalent to the optimal intervention in a setting where asset values and investment opportunities are known to the government.

We also study three extensions of the model. The first extension is to allow for heterogeneity of firm assets. This extension does not affect the government's cost of buying equity or providing debt guarantees but raises the cost of purchasing firm assets. The reason is that firms choose to sell their lowest quality assets to the government. The second extension is to allow for insurance of debt claims by the government. This extension is relevant for financial institutions to which the government provides deposit insurance. Deposit insurance decreases the cost of intervention because the government is partly reducing expected insurance payments. However, deposit insurance does not alter our results on the relative efficiency of the different interventions. The third extension is to allow for different structures of debt covenants. In our benchmark model, we assume that debt covenants prevent

banks from selling safe assets. If we weaken this assumption and allow for the sale of safe assets, the cost of asset purchases decreases because purchasing safe assets effectively gives priority to the government over debt holders.

This paper relates to the literature on government bailouts. Most of the literature on government bailouts focuses on financial institutions. Gorton and Huang (2004) argue that there is a potential role for the government to bail out banks in distress because the government can provide liquidity more effectively than the private market. Diamond and Rajan (2005) show that bank bailouts can increase excess demand for liquidity, which can cause further insolvency and lead to a meltdown of the financial system. Diamond (2001) emphasizes that governments should only bail out banks that have specialized knowledge about their borrowers. Aghion, Bolton, and Fries (1999) show that bank bailout policies can be designed such that they do not distort ex-ante lending incentives relative to strict bank closure policies. Kocherlakota (2009) analyzes resolutions to a banking crisis in a setup where insurance provided by the government generates debt overhang. He analyzes the optimal form of government intervention and finds an equivalence result similar to our symmetric information equivalence theorem. Our papers differ because we focus on debt overhang generated by the private sector and we consider the problem of endogenous selection into the government's programs. Debt overhang also plays a fundamental role in the model of Diamond and Rajan (2009).

The paper proceeds as follows. Section 1 sets up the model. Section 2 solves for the decentralized equilibrium with and without debt overhang. Section 3 describes the government interventions. Section 4 compares the interventions. Section 5 extends the model to heterogeneous assets and deposit insurance. Section 6 discusses optimal mechanisms. Section 7 discusses the financial crisis of 2007-2009. Section 8 concludes.

1 Model

Our model is applicable to firms and financial institutions alike but, for concreteness, we focus on financial institutions. For simplicity, we refer to all financial institutions as banks.

The model has a continuum of banks of measure 1. Figure 1 summarizes the timing, technology, and information structure of the model. The model has three dates $t = 0, 1, 2$.

There is no discounting. Banks start time 0 with given initial assets and liabilities. At time 1 banks receive new investment opportunities, and they lend to and borrow from each other and from outside investors. To avoid confusion with inter-bank lending, we use the word “investments” to refer to the new loans that banks make to the non-financial sector at time 1. All returns are realized at time 2, and profits are paid out to investors.

The government announces its interventions at time 0, but the implementation can happen either at time 0 or at time 1. The difference matters because banks learn about the value of their existing assets and about their new investment opportunities at time 1. Interventions at time 1 are therefore subject to adverse selection, while interventions at time 0 are not. The two cases are empirically relevant, and we therefore analyze both.

1.1 Initial assets and liabilities

At time 0 banks have both assets and liabilities in place. All banks are ex-ante identical. On the liabilities side, banks have long term debt. Long term debt is due at time 2. Let D be the face value of long-term debt outstanding.

On the asset side, banks have three types of assets: cash, safe long-term assets, and risky long-term assets. Cash is liquid and can be used for investments or for lending at time 1. Let c_t be cash holdings at the beginning of time t . All banks start time 0 with c_0 in cash. Cash holdings cannot be negative:

$$c_t \geq 0 \text{ for all } t.$$

Safe long-term assets deliver payoff \underline{A} at time 2. Risky long-term assets deliver random payoff $a = A$ or $a = 0$ at time 2. We define the probability of a good outcome as

$$p \equiv \Pr(a = A).$$

At time 1 private investors learn the value of p for each bank.

We focus on the binary outcome model because it delivers the main insights while simplifying the algebra. We will later extend our equivalence theorem to a general distribution for a . Note that any binary asset payoff can be modeled using the risky/safe asset model. For example, suppose that the payoffs are A in the good state and A in the bad state. To get back to the risky/safe model, we simply define $\underline{A} = A$ and $A = A - A$.

1.2 Investment opportunities

At time 1 banks receive investment opportunities. Investments cost the fixed amount x at time 1 and deliver income v at time 2. The value of v is between 0 and V and banks learn v at time 1. The joint distribution of p and v is

$$F(p, v) \text{ for } p \in [0, 1] \text{ and } v \in [0, V].$$

We define the unconditional mean of p as

$$\bar{p} \equiv E[p].$$

To make the problem interesting, we assume that individual banks do not have enough cash to finance investment projects. To study debt overhang, we assume that debt is risky such that long term debt D is in default when $a = 0$, but not when $a = A$. We also assume that the payoff v from new investment is not sufficient to cover long term debt D .

Assumption A1: $c_0 < x < V < D - \underline{A} < A$

Assumption A1 is maintained throughout the paper. Borrowing and lending at time 1 can be among banks, or between banks and outside investors. We assume risk neutral investors and we normalize the risk free rate to 0.

Assumption A2: Safe assets \underline{A} are protected by debt covenants

Assumption A2 protects debt holders from expropriation by equity holders. It is well known that equity holders have incentives to engage in risk shifting at the expense of debt holders. For instance, shareholders might decide to sell the safe assets and invest the proceeds in risky projects. Debt covenants protect debt holders. Debt covenants play an important role when we discuss asset buyback programs.

2 Equilibrium without intervention

In this section, we study the equilibrium without government intervention. We characterize the first best outcome, and the debt overhang equilibrium.

2.1 Investor payoffs

Figure 2 summarizes the payoffs to equity holders. In order to finance investment, banks can lend to and borrow from each other. Let l be the face value of borrowing at time 1 and let r be the gross interest rate for interbank lending. At time 2 total bank income y is:

$$y = \underline{A} + a + c_2 + v \cdot i,$$

where i is dummy for the decision to invest at time 1. Let y_d , y_l and y_e be the payoffs at time 2 of long term debt, interbank lending, and equity, respectively. Long term debt is senior to interbank lending l . Equity is junior to debt. There are no direct deadweight losses from bankruptcy. Under the usual seniority rules, the payoffs to investors are:

$$y_d = \min(y, D); \quad y_l = \min(y - y_d, rl); \quad y_e = y - y_d - y_l.$$

Under assumption A1, the payoffs to investors depend on the realization of asset value a in the following way. If $a = A$, all liabilities are fully repaid ($y_d = D$ and $y_l = rl$) and equity holders receive $y_e = y - D - rl$. If $a = 0$, then long term debt holders receive all income ($y_d = y$) and other investors receive nothing: $y_l = y_e = 0$.

2.2 First best

Figure 3 depicts the investment region in the first best equilibrium. Without intervention, the banks simply carry their cash holdings from period 0 to period 1, so $c_1 = c_0$. The interbank lending market opens at time 1. The first best assumption is that banks choose investments at time 1 to maximize total value $V_1 = \underline{A} + E_1[a] + c_2 + v \cdot i - E_1[y]$, subject to the time 1 budget constraint

$$c_2 = c_1 + l - x \cdot i. \tag{1}$$

The break even constraint for outside lenders is:

$$E_1[y] \geq l. \tag{2}$$

Using assumption A1, there is excess aggregate liquidity to finance the investment, and the break even constraint (2) binds: $E_1[y] = l$. Using (1), this implies that

$$V_1 = \underline{A} + E_1[a] + c_1 + (v - x) \cdot i.$$

Therefore, investment takes place in the domain:

$$I^* \equiv \{(p, v) \mid v > x\}.$$

Proposition 1 *The first best solution is for investment to take place at time 1 if and only if $v > x$, irrespective of the value of p .*

Two properties of the first best solution are worth mentioning. First, the interest rate is bank specific since equation (2) is simply $r = 1/p$. Second, there is a natural connection between maximizing shareholder value and maximizing total value. We can always write $V_1 = E_1 [y - y] = E_1 [y + y]$. The maximization program for total value is equivalent to the maximization of shareholder value $E_1 [y]$ as long as we allow renegotiation and transfer payments between shareholders and debt holders.

2.3 Debt overhang

We assume that banks maximize shareholder value instead of total value. Under the risky debt assumption A1, shareholder value maximization leads to the classic debt overhang problem.

Figure 4 depicts the investment region in the debt overhang equilibrium. Consider the market at time 1. Shareholders get nothing if the bad state realizes at time 2, and if the good state realizes they get $c_2 + \underline{A} + A + v \cdot i - D - rl$. The bank maximizes shareholder value subject to budget constraint (1) and break even constraint for new investors (2). The condition for investment becomes

$$v - x > (r - 1)l. \tag{3}$$

This is the investment condition under debt overhang.

Recall that the first best investment rule was simply $v - x > 0$. The difference with the first best investment rule comes from two critical properties. First, the outside investors ask for a risk premium because they know that lending is risky. Hence $r > 1$. Second, shareholders perceive a high cost of funds because they do not get the returns of the investment project in the bad state. In the first best world, they would renegotiate with the

debt holders. Debt overhang follows from the assumption that debt contracts cannot be renegotiated, or at least not quickly enough to seize the investment opportunity.

A constrained firm would always choose to invest its own cash first, so $c_2 = 0$, and $l = x - c_1$. Since $c_1 = c_0$, Equation (3) becomes $pv + (1 - p)c_0 > x$ and we get the investment domain:

$$I \equiv \{(p, v) \mid L(p, v) > 0\}, \quad (4)$$

where we define

$$L(p, v) \equiv pv + (1 - p)c_0 - x. \quad (5)$$

If $L(p, v) < 0$, no investment takes place. If $L(p, v) > 0$, investment takes place using the free cash c_0 and the additional borrowing $x - c_0$. The function $L(p, v)$ measures the value for shareholders of undertaking a new investment under debt overhang, given the quality of the existing assets p , the available cash c_0 , and the fundamental value of new investment v . From the perspective of shareholders, the NPV of the investment is $pv - x$. Internal cash c_0 has a lower opportunity cost than external financing because from the equity holder's perspective internal cash has an expected value of p but external financing has an expected cost of $pr = 1$.

2.4 Shareholder value and welfare losses

We repeatedly use the time 0 and time 1 equity value to compute equity holder's optimal investment and participation decisions. The equity value at time 1 is

$$E_1[y \mid p, v] = p(N + c_0) + L(p, v) 1_{(p, v) \in I} \quad (6)$$

where

$$N \equiv \underline{A} + A - D.$$

Equity value at time 1 is the sum of two terms. The first term is the equity holder's expected value of long term assets and cash minus senior debt. The value is multiplied by probability p because equity holders only receive a payment in the high-payoff state. The second term is the equity holder's value of new investment opportunities $L(p, v)$ as defined above.

Taking expectations at time 0, the equity value is:

$$E_0[y] = \bar{p}(N + c_0) + \int \int_o L(p, v) dF(p, v) \quad (7)$$

The first term is the expected equity value of long term assets and cash minus senior debt using the unconditional probability of solvency \bar{p} . The second term is the time 0 expected value of new investment opportunities. The domain I is defined in Equation (4). Since investment is chosen optimally, the value of new investment opportunities $L(p, v)$ is zero on the border of I .

Social welfare under debt overhang depends on the set of implemented investment projects I . We define $W(\cdot)$ as the social welfare function, so that welfare under debt overhang is

$$W(I). \quad (8)$$

As long as the second best investment set I is strictly smaller than the first best investment set I^* , there is a welfare loss. In the banking context, these deadweight losses are missed trading and lending opportunities. We assume the social welfare function incorporates deadweight losses to both banks and borrowers. Hence, the welfare function is independent of how the benefits of investment projects are shared among banks and borrowers.

Note that equation (8) assumes that investment projects are bank specific. This assumption is justified by the large literature in banking which argues that one of the main functions of financial intermediaries is to generate private information about their borrowers (see for instance Diamond (1984)), and that it is costly for borrowers to switch to other banks or other sources of funds.

3 Description of government interventions

We consider three government interventions: asset buy backs, cash against equity, and debt guarantees. We first discuss the government's objective function and then briefly describe each intervention.

3.1 Government objective function and constraints

The objective of the government is to minimize the welfare losses from missed investment opportunities and the costs of intervention. Let Ψ be the expected cost of a government

intervention. Let χ be the marginal deadweight losses associated with raising taxes and administering government interventions. The objective function of the government is

$$\max_{\Gamma} W(I(\Gamma)) - \chi \Psi(\Gamma)$$

where Γ are the parameters chosen by a specific government intervention. For simplicity, we assume that the marginal cost χ is constant. This means that the government cares about expected costs, but not about the distribution of these costs.

The expected costs of the program depend on the time of participation. At time 0, all banks are identical and information is symmetric. At time 1, the banks learn the value of their investment opportunities and the expected value of their long term assets. The type of a bank is a two-dimensional random variable (p, v) realized at time 1.

We place constraints on the interventions of the government. First, we do not allow the government to change the priority rules of financial contracts and we assume that the government cannot make debt holders worse off. These restrictions rule out government interventions such as forced bankruptcy, forced assets sales, and debt equity swaps, which would result in losses to debt holders. We also assume that the government cannot make payments directly contingent on the banks' new investments. This rules out directed lending. Finally, we assume that the government can restrict dividend payments to shareholders. Otherwise banks would simply pay out proceeds from government interventions as a dividend to shareholders.

3.2 Description of asset buy back program

The asset buy back program is parameterized by Z and p . The government announces at time 0 that it is willing to purchase risky assets up to an amount Z at a per unit price of p in exchange for cash. If a bank decides to participate and sell $z < Z$, long term assets become $A_1 = A - z$ and cash $c_1 = c_0 + zp$.

We note that the government can only buy risky but not safe long term assets. The reason is that under Assumption A2 debt covenants prevent equity holders from selling safe assets. This assumption is important because, as we show below, equity holders can extract rents from debt holders by selling safe assets. The intuition is that safe asset sales change the priority structure of financial claims and effectively give equity holders priority over

debt holders.

The government can offer banks to participate in the asset buy back program at time 0, at time 1, or at both times. The time of participation is important because at time 1 banks learn about the value of investment opportunities and the expected value of long term assets. Due to the option value of new information, banks always choose to wait with their decision until time 1 if possible. Without loss of generality, we thus only consider government programs with participation at either time 0 or at time 1, not at both times.

At time 0, we can without loss of generality consider programs where all banks participate because all banks are identical and the government can always set $Z = 0$. The expected cost of the time 0 asset buy back program is

$$\Psi_0(Z, p) = z_0(p - \bar{p}) \text{ with } z_0 < Z$$

where z_0 is the face value of assets purchased by the government. The government pays out $z_0 p$ at time 0 and receives z_0 in the high-payoff state with probability \bar{p} .

At time 1, the cost of the asset buy back program is different because banks learn the value of investment opportunity v and the value of long term assets p before deciding whether to participate. The expected cost is therefore

$$\Psi_1(Z, p) = \int \int z_1(Z, p; v, p) \cdot (p - \bar{p}) dF(v, p)$$

where z_1 is the face value of risky long term assets sold under the program. This formulation allows for adverse selection because banks may participate in the program depending on their type (v, p) .

3.3 Description of equity injection program

Equity injection programs are parameterized by m and α . The government announces at time 0 that it is willing to offer cash m against a fraction α of equity returns. Similar to the asset buy back program, the government can offer banks to participate in this program at time 0 or time 1. If a bank decides to participate, its cash position becomes $c_1 = c_0 + m$. The expected cost of the program at time 0 is

$$\Psi_0(m, \alpha) = m - \alpha E_0[y(m)]$$

where $E_0[y(m)]$ is the expected equity return at time 0 conditional on cash injection m . In words, the government pays out m at time 0 and receives a share α of equity returns y at time 2. There are no constraints on that program, except $m \geq 0$ and $\alpha \in [0, 1]$. The expected cost of the time 1 program is

$$\Psi_1(m, \alpha) = \int \int_{(\cdot)} \delta(m, \alpha; v, p) \cdot (m - \alpha E_1[y(m) | v, p]) dF(v, p)$$

where δ is an indicator variable whether a bank participates in the program, and $E_1[y(m) | v, p]$ is the expected equity return at time 1 conditional on cash injection m and bank type (v, p) . Similar to the asset buy back program, this formulation allows for adverse selection depending on bank type (v, p) .

3.4 Description of debt guarantee program

Debt guarantee programs are parameterized by S and ϕ . The government announces at time 0 that it is willing to guarantee new bank debt up to a face value of S and charges banks a fee ϕ per unit of lending. There are several equivalent ways to define the parameters S and ϕ . In our notation, the fee is paid up-front and the upper bound applies to the face value of new bank debt. Let s be the face value of new bank debt issued under the program and let r be the interest rate on debt issued under the program. The amount of money raised at time 1 is therefore $s/r - \phi s$ and the constraint is $s < S$ (we will see shortly that $r = 1$ in equilibrium). At time 0, the expected cost to the government is

$$\Psi_0(S, \phi) = s_0(1 - \phi - \bar{p}).$$

The expected cost to the government is the probability of the low-payoff state $(1 - \bar{p})$ minus the guarantee fee ϕ .

At time 1, the expected cost of the government is

$$\Psi_1(S, \phi) = \int \int_{(\cdot)} s_1(S, \phi; v, p) (1 - p - \phi) dF(v, p). \quad (9)$$

Similar to the other programs, the time 1 debt guarantee allows for adverse selection depending on bank type (v, p) .

4 Comparison of government interventions

Our main result is that all interventions are equivalent at time 0, but equity injections dominate both asset buy backs and debt guarantees at time 1. Equivalence of two interventions means that both interventions implement the same level of investment at the same expected cost to the government. Dominance of two interventions means that two interventions implement the same level of investment but the dominant intervention has a lower costs than the dominated intervention. To build the intuition for our result we first present two useful lemmas, one for providing free cash to banks and one for debt guarantees.

The following investment domain $I(m)$ plays a key role in our discussions.

Definition 1 *Let the domain $I(m)$ be defined by*

$$I(m) \equiv \{(p, v) \mid L(p, v) + (1 - p)m > 0\}. \quad (10)$$

4.1 Equilibrium with free cash injections at time 0

We first discuss the case of providing free cash to banks at 0. That is, the government simply gives cash m to each bank, without asking for anything in return. This case is a useful benchmark because it illustrates how free cash injections affect the investment region. In terms of the government programs, free cash injections are equivalent to an equity injection m with equity share $\alpha = 0$, an asset buy back program with face value $Z \rightarrow 0$ and cash injection $pZ = m$, and a debt guarantee program with face value $S = m$ and guarantee fee $\phi = 0$. The following lemma characterizes free cash injections.

Lemma 1 *A free cash injection leads to the following welfare function for the government*

$$W(I(m)) - \chi m$$

Proof. Suppose the government injects m in each bank so that initial liquidity becomes $c_1 = c_0 + m$. From equation (4) and (5), we see that the investment domain becomes $I(m)$ and the total cost is $\Psi_0(m, 0) = m$ since the number of banks is normalized to one. ■

Figure 5 shows the effect of the free cash injection on the investment region $I(m)$. The cash injection m relaxes the investment constraint and therefore expands the set of implemented investment projects. If the cash injection is large enough to cover the entire financing need $x - c_0$, then the cash injection can eliminate the entire debt overhang. In other words, $I(x - c_0) = I^*$.

4.2 Equilibrium with debt guarantee at time 1

We now discuss the equilibrium with a debt guarantee at time 1. The comparison of the debt guarantee with free cash injection illustrates the main incentive effects of government interventions. To compute the banks' optimal investment and participation decision, we use the expected equity value. We obtain the equity value at time 0 and time 1 by replacing c_0 by $c_0 + m$ and I by $I(m)$ in equations (6) and (7).

Banks benefit from the debt guarantee by the government because it allows them to issue riskless debt. The equilibrium interest rate on riskless debt is $r = 1$ and the equilibrium interest rate on unsecured debt $r = 1/p$. The time 1 budget constraint (1) becomes

$$c_2 = c_0 + l + (1 - \phi)s - x, \quad (11)$$

and the investment condition (3) becomes

$$L(p, v) + s(1 - \phi - p) > 0. \quad (12)$$

It is clear from the budget constraint (11) that the government never wants to set S above $x - c_0$ since this could not possibly help the financing of new investment opportunities.

Also note that the government wants to design an intervention such that banks only participate in the program if they invest. Otherwise, the program would provide a subsidy to banks that make no investments. As discussed above, we assume that the government does not observe new lending and therefore cannot make participation contingent on new investments. It is therefore important to impose a 'no inefficient participation' constraint (NIP from now on). Payoffs to equity holders in the good state are $A - D + c_2 - s$, so from equation (11) it is clear that the NIP constraint is:

$$\phi > 0. \quad (13)$$

We summarize this brief discussion in the following lemma.

Lemma 2 *It is enough to consider debt guarantees such that $S \in [0, x - c_0]$ and $\phi > 0$.*

Next we consider the choice between secured and unsecured borrowing. It is clear from (12) that banks take up the debt guarantee rather than the unsecured lending if and only if $p < 1 - \phi$. Otherwise, banks prefer borrowing on the unsecured interbank lending market. This defines an upper-bound schedule for participation, $U_1(p, v; S, \phi) < 0$, where:

$$U_1(p, v; S, \phi) \equiv p + \phi - 1. \quad (14)$$

Because of the upper bound, if $p \in [1 - \phi, 1]$, banks do not participate in the program. However, if the bank type $(p, v) \in I$, the bank invests even without the debt guarantee from the program.

If $p < 1 - \phi$, banks prefer to participate in the debt guarantee program. Since the payoffs are linear in s , banks choose the maximum guarantee: $s = S$. This implies unsecured borrowing $l = x - (1 - \phi)S - c_0$ if the banks invest. Equation (12) leads to the lower bound schedule for investment, $L_1(p, v; S, \phi) > 0$, where:

$$L_1(p, v; S, \phi) \equiv L(p, v) + (1 - \phi - p)S \quad (15)$$

We now have a complete description of the participation and investment decisions. The structure comprises four elements and this structure is the same for all government interventions.

First, there is an NIP constraint (13) which means that the program cannot be too generous. The NIP constraint is like a haircut and defines an upper-schedule (14) above which banks do not participate in the government intervention. In the case of the debt guarantee program, the upper-schedule is vertical (it does not depend on v), but in general it is a function of p and v (as in the case of cash against equity, see below).

Second, there is a lower-schedule (15) under which banks are unwilling to invest even with the assistance of the government. These banks do not participate in the program and do not invest. In the case of the debt guarantee program, the lower schedule is a function of the bank type (p, v) and the guarantee fee ϕ . The lower-schedule and the upper-schedule define the participation set:

$$\Omega_1(S, \phi) = \{(p, v) \mid L_1(p, v; S, \phi) > 0 \wedge U_1(p, v; S, \phi) < 0\} \quad (16)$$

Third, the lower-schedule defines the investment domain. The investment domain is the combination of the initial debt overhang set I^0 (banks that would invest even without the government's intervention) and the participation set $I_1^g(S; \gamma)$:

$$I_1^g(S; \gamma) = I^0 \cup I_1^g(S; \gamma) \quad (17)$$

Note that the overlap between the two sets, $I^0 \cap I_1^g(S; \gamma)$, represents opportunistic participation. Opportunistic participation is inefficient, because the government provides a subsidy to banks that would have invested even in the absence of the government intervention.

Fourth, the participation set determines the expected cost of the government intervention. Using equation (9), the expected cost of the debt guarantee program is

$$I_1^g(S; \gamma) = \int_{S \in I_1^g(S; \gamma)} \int_{\gamma} (1 - p) dF(p; v) \quad (18)$$

Figure 6 shows the investment set and participation set for debt guarantees provided at time 1. The figure distinguishes three regions of interest: efficient participation, opportunistic participation, and invest alone. The efficient participation region comprises the banks that participate in the intervention and that invest because of the intervention. The opportunistic region comprises the banks that participate in the intervention but would have invested even in the absence of the intervention. The invest alone region comprises the banks that do not participate in the program and invest without government intervention. As is clear from the figure, the government's trade-off is between expanding the efficient participation region and reducing the opportunistic participation region.

We summarize these results in the following lemma:

Lemma 3 A time 1 debt guarantee program $(S; \gamma)$ delivers welfare function $W(I_1^g(S; \gamma))$ and has the expected cost $I_1^g(S; \gamma)$:

We can compare the debt guarantee with the free cash injections:

Proposition 2 Debt guarantees at time 1 always dominate free cash injections at time 0.

Proof. Consider a debt guarantee with $\phi = 0$ and $S = m$. Both interventions achieve the same investment domain since $I_1(m, 0) = I(m)$. However, the participation set for the time 1 debt guarantee is smaller than the participation set of the free cash injection. As a result, the expected cost of the debt guarantee $\Lambda_1(m, 0)$ is smaller than the expected cost of the free cash injection m . ■

In general, we see that debt guarantees are less costly than free cash injections because of three separate reasons. First, the NIP constraint ensures that only banks that invest participate in the debt guarantee program but with free cash injections also banks that do not invest participate in the program. Second, under the debt guarantee program the government only pays out insurance if the bank defaults and is compensated by fee ϕ otherwise but under free cash injection the government always pays out cash. Third, under the debt guarantee some healthy banks invest alone without participating in the program, but all banks participate in the free cash injection.

We also note that risk shifting plays an important role in our model. Even though we assume that v is known at time 1, equity holders have an incentive for risk shifting. Indeed, from the perspective of shareholders, selling risky assets is similar to anti-risk-shifting, and refusing to sell assets is like risk shifting.

4.3 Comparison of time 0 programs

We now compare government programs at time 0. In these programs, the banks must opt in or out at time 0, when information is symmetric. We have the following proposition:

Theorem 1 *Equivalence of time 0 programs - binary model.* *A time 0 risky asset buy back program (Z, p) is equivalent to a time 0 debt guarantee program with $S = Z$ and $p = 1 - \phi$. It is also equivalent to a time 0 equity injection (m, α) , where $m = Zp$ and p and α are chosen such that at time 0 all banks are indifferent between participating and not participating in the program. All programs deliver the same investment set $I(m)$ and have the same expected costs*

$$\Lambda_0(m) \equiv (1 - \bar{p})m - m \int \int_{(\cdot)} (1 - p) dF(p, v) - \int \int_{(\cdot) \setminus \circ} L(p, v) dF(p, v) \quad (19)$$

Proof. See Appendix. ■

The key to this equivalence result is that banks are forced to decide to participate in the programs before they receive information about investment opportunities and asset values. Banks are thus identical and the government optimally chooses the program parameters such that banks are indifferent between participating and not participating. For a fixed program amount, the government extracts all rents from the intervention. The cost to the government is thus independent of whether banks are charged through assets sales, guarantee fees, or equity shares.

It is important to emphasize that we are comparing pure time 0 interventions here, where no further interaction between the banks and the government occurs at time 1. We are not claiming that these pure time 0 interventions are optimal. In fact, they are not. It is always better for the government to sell at time 0 an option to participate in a time 1 program. We return to this idea later.

It is also important to understand the cost function $\Lambda_0(m)$ by looking at the three terms on the RHS of equation (19). The first term reflects the fact that, in the bad state, the cash injection is received by long-term debt holders. The second term is the gain in borrowing costs conditional on being in the investment set. The third term is the subsidy to new investments. It contributes positively to the cost since $L(p, v) < 0$ for all $(p, v) \in I(m) \setminus I$. Note that $\Lambda_0(m) > 0$ since the first term dominates the second and the third is positive.

We can now discuss the role of assumption A2.

Proposition 3 *Safe assets sale.* *If we relax Assumption A2, a program to sell $\underline{Z} < \underline{A}$ safe assets at time 0 in exchange for cash m has an expected cost of $\Lambda_0(m) - (1 - \bar{p})\underline{Z}$.*

The intuition is that a sale of *safe* assets changes the priority structure of financial claims. In the bad state, the government receives payoff \underline{Z} which would otherwise have gone to the debt holders. This transfer from the debt holders lowers the cost for the government. This discussion shows that selling safe assets is yet another way to get around the renegotiation issue. But note that this is unlikely to be efficient from an ex-ante perspective, since covenants to protect debt holders are valuable only if they are credible.

In market value terms, debt holders do not lose, as long as $m \geq \underline{Z}$. If \underline{Z} is high enough, then the government can implement $m = \underline{Z}$ and the cost becomes

$$-m \int \int_o (1-p) dF(p, v) - \int \int_{() \setminus o} (L(p, v) + (1-p)m) dF(p, v),$$

which is negative. In this case, the government would make money by capturing some of the rents. The debt holders break even if the firm does not invest since $m = \underline{Z}$, and are strictly better off if the firm invest since $v > m = \underline{Z}$. Of course, in practice it is difficult to separate assets just as it is difficult to do project financing. We do not argue that this is a realistic case, but we find it helpful to understand the nature of the economic problem.

We can further extend the model to allow for a continuous asset distribution instead of the binary setup. Suppose at time 1, banks learn the parameter $p \in [0, 1]$ and update the distribution to $G(\cdot|p)$ over the support $[0, A]$ for all p . The ex-ante distribution of (p, v) is $F(p, v)$, so the ex-ante distribution of a is

$$f_0(a) = \int_{=0}^1 \int_{=0} g(a|p) dF(p, v).$$

To compare the interventions, we need to define debt covenants for a continuous asset distribution. We assume covenants are efficient in the sense that for any distribution function F debt holders receive at least the expected payoff they would receive without asset buy backs. This assumption ensures that debt holders have priority over asset buy backs.

We also need to define the priority structure of junior creditors and debt issued under the debt guarantee. We assume that junior creditors are senior to debt issued under the debt guarantee. This assumption ensures that the government does not create its own debt overhang.

Theorem 2 *Equivalence of time 0 programs - continuous distribution case. A time 0 equity injection is equivalent to a time 0 asset buy back program with efficient covenants and equivalent to a time 0 debt guarantee program in which junior creditors have priority over guaranteed debt.*

Proof. See Appendix. ■

We think the generalization of the equivalence theorem to the continuous asset case is helpful for two reasons. First, and most importantly, we show that the equivalence theorem holds for the continuous asset case under reasonable specifications for debt covenants and debt guarantees.

Second, the continuous asset case clarifies the importance of the priority structure in designing government interventions. This is helpful because in the binary model all claims other than senior debt are either completely paid off or not paid at all.

Specifically, for debt guarantees the guaranteed debt has to be junior to borrowing at time 1. Under this assumption, the debt issued under the debt guarantee is effectively equivalent to buying preferred shares in the bank. The intuition is that the equivalence theorem holds as long as guaranteed debt does not generate its own debt overhang and therefore does not affect borrowing costs at time 1.

Similarly, efficient covenants ensure that senior debt holders have priority over asset buy backs. This assumption is equivalent to the covenant assumption A2 in the binary model. As discussed above, without covenants, the government can alter the priority structure by buying safe assets. We do not want to rule out such an intervention but we think ex-ante debt holders have strong incentives to demand efficient debt covenants. Hence, efficient debt covenants generate a priority structure for asset buy backs that is equivalent to the two other interventions.

4.4 Comparison of time 1 programs

Let us now compare the time 1 programs. In these programs, the banks must opt in or out at time 1, when information is asymmetric. We have the following proposition:

Theorem 3 *Equivalence of asset buy-backs and debt guarantees at time 1. An asset buy back program (Z, p) with participation at time 1 is equivalent to a debt guarantee program with $S = Z$ and $p = 1 - \phi$.*

Proof. See Appendix. ■

Note that the allocation features adverse selection, such that banks only participate in the program if the expected value of their assets p is less than the price p offered by the

government. This feature of the solution is a natural outcome of a setup in which banks know more about asset values than the government. The frequently made argument that asset buy backs or cash against equity have to occur at fair market value is not feasible because banks only participate in the program if the the program recapitalizes at rates above market value.

Theorem 4 *Dominance of equity injection at time 1.* *For any asset buy back program (Z, p) with participation at time 1, there is an equity program that achieves the same allocation at a lower cost for the government.*

Proof. See Appendix. ■

Figure 7 depicts the equilibrium with equity injection at time 1. The intuition is the following. First, we must understand the net effects of dilution. They are captured by the function

$$X(p; m, \alpha) \equiv (1 - \alpha) m - \alpha p (N + c_0).$$

This function is intuitive: $(1 - \alpha) m$ is the net value of cash injected by the government, and $\alpha p (N + c_0)$ is the dilution of the claims on old assets. So X measures the cash value of government transfers under the program. The participation set in the equity program takes the form

$$\Omega_1(m, \alpha) = \{(p, v) \mid L_1(p, v; m, \alpha) > 0 \wedge U_1(p, v; m, \alpha) < 0\}.$$

This can be compared to the participation set in equation (16). The lower bound is defined by

$$L_1(p, v; m, \alpha) \equiv (1 - \alpha) L(p, v) + X(p; m, \alpha).$$

We note that X is the cash transfer and $(1 - \alpha) L(p, v)$ is the diluted value of new investments. It is optimal to opt in and invest if $L_1(p, v; m, \alpha) > 0$. The upper bound for participation is

$$U_1(p, v; m, \alpha) \equiv \alpha L(p, v) - X(p; m, \alpha).$$

By not participating, the firm foregoes the transfers $X(p; m, \alpha)$ but avoids the dilution of its new project. Hence, it is optimal to invest without the assistance of the government

when $U_1(p, v; m, \alpha) > 0$. Finally, the NIP constraint is

$$X(1; m, \alpha) < 0.$$

The NIP constraint ensures that the government does not provide cash to banks that do not plan to invest. In this case, the cash is transferred one for one between the good and the bad state, so the condition is $(1 - \alpha)m < \alpha(N + c_0)$. This condition is the same as $X < 0$ for banks whose assets are safe, i.e., the banks for which $p = 1$. It also means that $X(p; m, \alpha) \leq (1 - \alpha)(1 - p)m$ and therefore the investment domain is strictly smaller than in the pure cash injection: $I_1(m, \alpha) \subset I(m)$. The reason is that firms with high p and low v opt out to avoid dilution.

To understand why equity injections are better than the other interventions, consider a given asset buy back program. It has a lower schedule that determines the investment set, and thus the welfare function W . Now choose the equity program to have exactly the same lower schedule and thus the same investment set as the asset buy back program.

The first point to understand is that equity injections induce less opportunistic participation. This is because it is costly for good banks to dilute their valuable equity. Hence the upper schedule is tighter. Of course, the two programs have different cost functions, so the fact that the participation set is smaller is not enough to show that equity injections are cheaper than asset buy backs. However, the same reasons that make the upper schedule tighter also limit the rents earned as (p, v) move away from the lower frontier $L_1(p, v; m, \alpha) = 0$. Finally, it is easy to show that, once the lower schedules are the same, the NIP constraints are also equivalent. This shows that, for any asset buy back, or any debt guarantee program, there exists an equity injection program that delivers exactly the same investment set, but for a lower cost to the government. The lower cost comes from two sources: less opportunistic participation and smaller rents conditional on participation.

4.5 Time 0 versus time 1

Let us now compare the programs at times 0 and 1. From the perspective of the government, at time 0 there is adverse selection with respect to p since banks with bad assets are more likely to participate. There is also beneficial selection with respect to v since banks without investment projects are less likely to participate. We consider a change in the distribution

of both p and v .

Proposition 4 *Comparison of time 0 and time 1 programs.*

- Consider two distribution functions F and \tilde{F} for the parameters (p, v) . If \tilde{F} dominates F in the sense of first order stochastic dominance, then, for any investment domain I , the cost of the time 0 program is lower with \tilde{F} than with F .
- Time 1 programs always dominate time 0 programs when few banks have positive NPV projects (i.e., $\Pr(v > x) \rightarrow 0$).
- Time 0 programs always dominate time 1 programs when most banks have positive NPV projects (i.e., $\Pr(v > x) \rightarrow 1$) and the government wants to implement a large program ($m \rightarrow x - c_0$, $I \rightarrow I^*$)

Proof. See Appendix. ■

To understand the first result, note that a first order stochastic dominance shift increases the likelihood that banks will be in the investment region. Banks in the investment region invest because the equity value is larger with investment than without investment. Since the government extracts all surplus from investment and the costs of time 0 programs are independent of the distribution $F(p, v)$, a first order stochastic dominance shift always reduces the cost of government intervention at time 0.

To understand the second result, note that for every asset buy back program at time 0, we can construct an asset buy back program at time 1 that generates the same investment region by setting the asset price p at time 1 equal to one and choosing time 1 program size Z such that it generates the same cash injection as the time 0 asset buy back program. If $\Pr(v > x) \rightarrow 0$ no bank receives an investment opportunity. Hence, there is no investment under any program. However, a time 0 asset buy back program yields a positive cost (because all banks participate) and a time 1 program yields zero cost (because nobody participates).

As more banks receive good investment opportunities, the cost of the time 0 program decreases because it extracts all rents from better investment opportunities. In contrast, the

cost of time 1 asset buy backs increases because more banks participate and participating banks receive informational rents. This trade-off explains the third result.

A natural interpretation of time 0 versus time 1 is in terms of compulsory versus voluntary participation. Of course, compulsory participation without constraint does not make sense, so we impose the constraint that government offers have to be acceptable on average (for instance, a well diversified equity investor would accept the offer on behalf of all the banks). Our results can then be interpreted as follows: when interventions are large, and the government expect that most banks have positive NPV projects (positive franchise value), then it is better to do it early with compulsory participation. On the other hand, when interventions are small, or if most banks do not have valuable new projects, then it is better to do it ex-post based on voluntary participation.

5 Extensions

5.1 Heterogeneous assets within banks

We consider an extension of our model to allow for asset heterogeneity within banks. Suppose that the face value of assets at time 0 is $A + A'$. All these assets are ex-ante identical. At time 1, the bank learns which assets are A' and which assets are A . The A assets are just like before, with probability p of A and $1 - p$ of 0. The A' assets are worth zero with certainty. The ex-ante problems are unchanged, so all programs are still equivalent at time 0.

The equity and debt guarantee programs are unchanged at time 1. So equity still dominates debt guarantee. But the asset buy back program at time 1 is changed. For any price $p > 0$ the banks will always want to sell their A' assets. This will be true in particular of the banks without profitable lending opportunities.

Proposition 5 *With heterogeneous assets inside banks, there is a strict ranking of programs: equity is best, debt guarantee is intermediate, buy back program is worse.*

The main insight from this extension is that adverse selection across banks is different from adverse selection across assets within banks. Adverse selection within banks increases the cost of the asset buy back program but does not affect the other programs.

Corollary 1 *For asset buy backs to be optimal, the market failure must come from private information among private agents.*

Of course, this is only a necessary condition. It remains to be seen if and how an asset buy back program can be optimal in the case of adverse selection in the private sector (Philippon and Skreta (2009)).¹

5.2 Deposit Insurance

Suppose long term debt consists of two types of debt: deposits Δ and unsecured long term debt B such that

$$D = \Delta + B.$$

Suppose that the government provides insurance for deposit holders and that deposit holders have priority over unsecured debt holders. Then the payoffs are are:

$$y^\Delta = \min(y, \Delta); y^- = \min(y - y^\Delta, B)$$

We consider two separate cases. The first case is safe deposits if $\Delta < \underline{A} + c_0$ and the second case is risky deposits if $\Delta \geq \underline{A} + c_0$.

Proposition 6 *With safe deposits, the cost and benefits of both time 0 and time 1 programs remain unchanged.*

Proof. See Appendix. ■

If deposits are safe, banks always have sufficient time 2 income to repay deposit holders. Hence, the expected cost of deposit insurance is zero independent of whether there is a government intervention. As a result, the costs and benefits of all programs remain unchanged.

Proposition 7 *With risky deposits, the costs of time 0 and time 1 programs decrease. The equivalence results and ranking of both time 0 and time 1 programs remain unchanged. If deposits are sufficiently large, time 0 programs dominate time 1 programs and the government can implement the first best at negative cost.*

¹It is worth pointing out that adverse selection can be mitigated by debt overhang. In our simple model, the maximization of shareholder value does not create adverse selection because a fixed rate would not attract the low type (low p). By contrast, total firm value maximization would lead to adverse selection. Hence it is clear that the two market failures are best studied in separate models.

Proof. See Appendix. ■

With risky deposits, the government has to pay out deposit insurance in the low-payoff state. Hence, every cash injection at time 0 lowers the expected cost of deposit insurance in the low-payoff state one-for-one. As a result, the government recoups its entire investment both in the high- and low-payoff state. Put differently, the time 0 cash injection represents a wealth transfer to depositors and, because of deposit insurance, a wealth transfer to the government. Also note that the government extracts all benefits of increased lending ex-ante by keeping equity holders to their reservation utility. As a result, the government receives the expected net benefit of increased lending and thus the expected cost is negative.

6 Optimal programs

In this section, we characterize the constrained optimal intervention. The two constraints faced by the government are its inability to force debt holders to renegotiate outside bankruptcy, and its inability to observe the types of banks. We note that the government cannot overcome the second constraint by learning about asset values and investment opportunities from observed asset prices such as equity prices and credit default swap prices. The reason is that assets prices also reflect the perceived likelihood of future government interventions, so the government cannot use these prices to learn about the fundamental values that would prevail without intervention. Interestingly, however, we will show that the constrained optimal intervention implements the same outcome as if the government knew asset values and investment opportunities.

6.1 Time 0

Proposition 8 *Any time 0 program can be improved by making participation at time 1 voluntary and selling at time 0 the option to participate at time 1.*

Proof. See Appendix. ■

A practical example is the debt guarantee program. It is inefficient to force banks to issue S at time 0. It is better to sell them at time 0 the right to issue secured debt at time 1. In this way, banks who end up without investment opportunities do not participate, banks

who can invest alone also do not participate, and everyone pays at time 0 the present value of the option to participate.

Corollary 2 *An optimal time 0 program is to sell at time 0 the option to participate in an optimal time 1 program.*

6.2 Time 1

The following proposition extends the result of Theorem 4

Proposition 9 *Equity programs at time 1 cannot be improved by mixing them with a debt guarantee or asset buy back program. Pure equity programs always dominate.*

Proof. See Appendix. ■

We now consider optimal programs. The constraints we impose are that the debt holders cannot be worse off and that the government cannot alter the priority of claims. Hence, the government can inject cash m at time 1 in exchange for state contingent payoffs at time 2. Junior creditor at time 1 must be repaid, so assuming the government can commit to repay junior creditors, we can without loss of generality restrict our attention to the case where the government payoffs depend on the residual payoffs $y - y - y$.

In general, however, the government could offer a menu of contracts to the banks. A menu of contracts can be used to obtain various investment sets. The optimal choice depends on the distribution of types $F(p, v)$ and the welfare function W so we cannot say in general which set is optimal. However, we can examine cost minimization for any given investment set. This is what we do now.

Lemma 4 *Any program with voluntary participation of shareholders over the set Ω and no renegotiation with debt holders has a minimum cost of*

$$\Psi^{\min}(\Omega) = - \iint_{\Omega} L(p, v) dF(p, v)$$

Proof. Voluntary participation means that shareholders must get at least $p(N + c_0)$. With no renegotiation with debt holders, the government and old equity holders must share

the residual surplus whose value is

$$p(N + c_0) + L(p, v)$$

Hence the expected net payments to the government must be $\iint_{\Omega} L(p, v) dF(p, v)$. These are negative as long as Ω extends the debt overhang investment set, hence the positive minimum cost. ■

To understand this result, suppose the government can make type contingent offers conditional on new investments. For type (p, v) , the net value of new investment is $L(p, v)$ which is negative outside the I region. So the minimum the government has to pay such that it is optimal for type (p, v) to invest is $-L(p, v)$.

Proposition 10 *Consider the program $\Gamma = \{m, h, \varepsilon\}$ where the government offers a junior loan m at time 1 at the rate h in exchange for $(1 - \varepsilon)/\varepsilon$ warrants at the strike price $N + c_0$. This implements the investment set*

$$I(\Gamma) = I_1(S, \phi)$$

if we identify the cash injection $m = (1 - \phi)S$ and the haircut $h = \phi/(1 - \phi)$. In the limit $\varepsilon \rightarrow 0$, opportunistic participation disappears:

$$\lim_{\varepsilon \rightarrow 0} U(\Gamma) = L$$

Finally the program achieves the minimum cost in the limit:

$$\lim_{\varepsilon \rightarrow 0} \Psi(\Gamma) = \Psi^{\min}(I(\Gamma) \setminus I)$$

Proof. See Appendix. ■

Figure 8 depicts the equilibrium under the efficient mechanism. The intuition is that the payoff structure to old shareholders is now:

$$f(y) = \min(y, N + c_0) + \varepsilon \max(y - N - c_0, 0)$$

Old shareholders are full residual claimants up to the face value of old assets $N + c_0$ and ε residual claimants beyond. A few properties are worth mentioning. First, the loan must

be junior to all creditors but senior to common stock holders. Hence it could also be implemented with preferred stock. It is crucial, however, that the government also takes a position that is junior to shareholders. Dilution should happen on the upside to induce participation of firms who need it, and to limit opportunistic participation.

The use of warrants also has some advantages that are likely to be important for reasons outside the model. The first advantage is that it limits risk shifting incentives since the government owns the upside, not the old shareholders (see, for instance, Green (1984)). Second, the government can credibly commit to protecting the shareholders since it owns equity warrants. This is important because, conditional on not failing a bank, it makes no sense to try and punish the shareholders.

In practice, there might be lower bound on ε . It might be necessary to limit dilution to avoid fears of nationalization. An approximate optimal program would then be to determine first the minimum value of ε , and then to construct the program accordingly. Also the haircut h is chosen to rule out inefficient participation (the NIP constraint). In theory, any $h > 0$ would work, but in practice, parameter uncertainty would prevent h from being too close to zero.

7 Discussion of financial crisis of 2007/09

The financial crisis of 2007-2009 has underlined the importance of debt overhang. There is agreement among many observers that debt overhang is an important reason for the decline in lending and investment during the crisis (see Allen, Bhattacharya, Rajan, and Schoar (2008) and Fama (2009), among others).

For example, Ivashina and Scharfstein (2008) show that new lending was 68% lower in the three-month period around the Lehman bankruptcy relative to the three-month period before the Lehman bankruptcy. Using cross-sectional variation in bank access to deposit financing, the authors show that the reduction in lending reflects a reduction in credit supply by banks rather than a reduction in credit demand by borrowers.

The crisis has also shown the difficulty of finding effective solutions to the debt overhang problem. Several experts have expressed concerns that existing bankruptcy procedures for financial institutions are insufficient for reorganizing the capital structure. As an alterna-

tive, Zingales (2008) argues for a law change that allows for forced debt-for-equity swaps. Coates and Scharfstein (2009) suggest to restructure bank holding companies instead of bank subsidiaries. Ayotte and Skeel (2009) argue that Chapter 11 proceedings are adequate if managed properly by the government. Assuming that restructuring can be carried effectively, these approaches reduce debt overhang at low cost to the government. However, Swagel (2009) argues that the government lacks the legal authority to force restructuring and that changing bankruptcy procedures is politically infeasible once banks are in financial distress.

Moreover, concerns for systemic risk and contagion make it difficult to restructure financial balance sheets in the midst of a financial crisis. Aside from the costs of its own failure, the bankruptcy of a large financial institution may trigger further bankruptcies because of counterparty risks and runs by creditors. For example, Heider, Hoerova, and Holthausen (2008) emphasize the role of counterparty risk in the interbank market.

The government may therefore decide to avoid restructuring because there is a positive probability of a breakdown of the entire financial system. Even if the government decides to let some institutions restructure, the government also has to address debt overhang among the financial institutions that do not restructure. In fact, even proponents of restructuring suggest to rank banks based on their financial health and only restructure banks below a cut-off. Hence, independent of whether the government restructures some banks, the optimal form of government intervention outside restructuring remains an important question.

Surprisingly however, while there is at least some agreement regarding the diagnostic (debt overhang), there is considerable disagreement about the optimal form of government intervention outside restructuring. The original bailout plan proposed by former Treasury Secretary Paulson favors asset buy backs over other forms of interventions. Stiglitz (2008) argues that equity injections are preferable to asset buy backs because the government can participate in the upside if financial institutions recover. Soros (2009a) also favors equity injections over asset buy backs because otherwise banks sell their least valuable assets to the government. Diamond, Kaplan, Kashyap, Rajan, and Thaler (2008) argue that the optimal government policy should be a combination of both asset buy backs and equity injections because asset buy backs establish prices in illiquid markets and equity injections encourage new lending. Bernanke (2009) suggests that in addition to equity injections and debt

guarantees the government should purchase hard-to-value assets to alleviate uncertainty about bank solvency. Geithner (2009) argues that asset buy backs are necessary because they support price discovery of risky assets.

Other observers have pointed out common elements among the different interventions without necessarily endorsing a specific one. Ausubel and Cramton (2009) argue that both asset buy backs and equity injections require to put a price on hard-to-value assets. Bechuk (2008) argues that both asset buy backs and equity injections have to be conducted at market values to avoid overpaying for bad assets. Soros (2009b) argues that bank recapitalization has to be compulsory rather than voluntary. Kashyap and Hoshi (2008) compare the financial crisis of 2007-2009 with the Japanese banking crisis and argue that in Japan both asset buy backs and capital injections failed because the programs were too small. Scharfstein and Stein (2008) argue that government interventions should restrict banks from paying dividends because, if there is debt overhang, equity holders favor immediate payouts over new investment. Acharya and Backus (2009) suggest that public lender of last resort interventions would be less costly if they borrowed some of the standard tools used in private contracts for lines of credit.

We believe our results in this paper make three contributions to this debate. First, we believe an analytical approach to this question is helpful because it allows the government to implement a principled approach in which financial institutions are treated equally and government actions are predictable. This approach is preferable to a trial-and-error approach in which the government adjust interventions depending on current market conditions and tailors interventions to requests of individual financial institutions. In fact, such a trial-and-error approach may create more uncertainty for private investors, which makes them even less willing to invest. Uncertainty also generates an option to wait for future interventions, which further undermines private recapitalizations. Moreover, tailor-made interventions are more likely to be influenced and distorted by powerful incumbents (see Hart and Zingales (2008), Johnson (2009)).

Second, we distinguish the economic forces that matter from the ones that do not by providing a benchmark in which the form of government interventions is irrelevant. Under symmetric information, all interventions implement the same level of lending at the same expected costs. In contrast, under asymmetric information buying equity dominates other

forms of intervention because buying equity reduces the extent of adverse selection across banks. Our analysis also shows how the government can use warrants to minimize the expected cost to taxpayers, an important element which has not been emphasized in the public debate on the financial crisis. Interestingly, Swagel (2009) notes that the terms of the Capital Purchase Program, the first round of government intervention, consisted of providing a loan in exchange for preferred shares and warrants. This structure is qualitatively consistent with the optimal intervention.

Third, our analysis clarifies why government interventions are costly. Under symmetric information, equity holders are held to their participation constraint but debt holders receive an implicit transfer. Hence, the same economic force that generates debt overhang in the first place, also generate the cost to the government. Under asymmetric information, participating banks receive rents because otherwise they would choose not to participate. Hence, under asymmetric information government interventions are costly because the government has to recapitalize at above market rates.

Finally, we note that our analysis does not address why the banking system entered financial distress and whether government bailouts affect future bank actions. In our model, we take the debt overhang as given and rely on other research that links the financial crisis to securitization (Mian and Sufi (2008), Keys, Mukherjee, Seru, and Vig (2010)) and the tendency of banks to become highly levered (Adrian and Shin (2008), Acharya and Schnabl (2009)). Regarding the impact of government interventions on future bank actions, we recognize that bailouts can create expectations of future bailouts which may cause moral hazard. However, if the government decides to intervene, then it is optimal for the government to choose the intervention with the lowest costs. In addition, the optimal intervention minimizes the rents to equity and debt holders, so the optimal intervention also minimizes moral hazard concerns conditional on the decision to intervene.

8 Conclusion

In this paper we study the efficiency and welfare implications of different government interventions in a standard model with debt overhang. We consider asset buy backs, cash against equity injections, and debt guarantees. We find that under symmetric information,

all interventions are equivalent. Under asymmetric information between the government and the private sector, equity injections dominate both asset buy backs and debt guarantees, and buyback programs are strictly worse when there is adverse selection within banks, in addition to adverse selection across banks.

Comparing voluntary and compulsory programs, we find that compulsory programs are more likely to be efficient if the intervention is large. We also show that deposit insurance reduces the expected cost of all government interventions. In the limit case in which deposits are always risky, the benefit of a bailout accrues to the government itself and the optimal solution is therefore to implement the first best at negative expected cost. Finally, we solve for the optimal mechanism. We find that the government should provide a subordinated loan (or buy preferred stock) in exchange for warrants.

Proof of Theorem 1

We show the equivalence result in the case of a binary distribution for asset value a .

Cash against equity

The government offers cash m against fraction α of equity capital. The investment domain $I(m)$ is the same as in the case of pure cash injections. At time 0, shareholders participate in the intervention if

$$(1 - \alpha) E_0 [y(m)] \geq E_0 [y(0)]. \quad (20)$$

The cost of the program to the government is

$$\Psi_0(m, \alpha) = m - \alpha E_0 [y(m)].$$

Because the investment domain does not depend on α , the government chooses equity share α such that the participation constraint (20) binds. Expected shareholder values at time 0 are

$$\begin{aligned} E_0 [y] &= \bar{p}(N + c_0) + \iint_{\circ} L(p, v) dF(p, v), \\ E_0 [y(m)] &= \bar{p}(N + c_0 + m) + \int \int_{(\cdot)} (L(p, v) + (1 - p)m) dF(p, v). \end{aligned}$$

Using the participation constraint (20) to eliminate α from the cost function yields

$$\Psi_0(m, \alpha) = m - (E_0 [y(m)] - E_0 [y])$$

with

$$E_0 [y(m)] - E_0 [y] = \bar{p}m + m \int \int_{(\cdot)} (1 - p) dF(p, v) + \int \int_{(\cdot) \setminus \circ} L(p, v) dF(p, v).$$

The expected cost of the optimally designed program is $\Lambda_0(m)$ defined in equation (19).

Asset buy back

Under the asset buy back program, we have $c_1 = c_0 + Zp$. Hence the investment domain becomes $I(Zp)$. The expected shareholder value at time 0 is

$$E_0 [y(z, p)] = \bar{p}(N + c_0 - (1 - p)Z) + \int \int_{(\cdot, z)} (L(p, v) + (1 - p)Zp) dF(p, v).$$

Shareholders participate in the program if

$$E_0 [y(Z, p)] \geq E_0 [y(0, 0)]. \quad (21)$$

Because the investment domain only depends on the total repurchase amount Zp , the government chooses to satisfy participation constraint (21) with equality. As a result, the participation constraint (21) yields

$$\bar{p}(1-p)Z = Zp \int \int_{(z)} (1-p) dF(p, v) + \int \int_{(z) \setminus o} L(p, v) dF(p, v).$$

Therefore the cost to the government is

$$\begin{aligned} \Psi_0(Z, p) &= Zp - Z\bar{p} \\ &= (1-\bar{p})Zp - Zp \int \int_{(z)} (1-p) dF(p, v) - \int \int_{(z) \setminus o} L(p, v) dF(p, v) \\ &= \Lambda_0(Zp). \end{aligned}$$

The program is equivalent to cash against equity when $m = Zp$.

Debt guarantee

Under the program $c_1 = c_0 + (1-\phi)S$. Hence the investment domain becomes $I((1-\phi)S)$. The expected shareholder value at time 0 is

$$E_0[y(S, 1-\phi)] = \bar{p}(N + c_0 - \phi S) + \int \int_{((1-\phi)S)} (L(p, v) + (1-p)(1-\phi)S) dF(p, v)$$

This is equivalent to the asset buy back program if we set $S = Z$ and $p = 1-\phi$.

Proof of Theorem 2

We show the equivalence result in the case of a general distribution for asset value a .

No intervention

As a benchmark, we first solve the debt overhang model without government interventions. Banks invest if

$$\begin{aligned} E[y|p, 1] &\geq E[y|p, 0] \\ \int_{+}^{-} (a - D + v - rl) dG(a|p) &\geq \int_{-}^{-} (a - D + c) dG(a|p) \end{aligned}$$

which is equivalent to

$$v - rl > c \iff v - c > r(x - c) \iff v - x > (r - 1)(x - c).$$

This investment decision is the same condition as in the binary payoff model. The break even constraint for junior creditors is

$$\begin{aligned} E[y|p] &\geq l \\ rl \int_{+}^{-} dG(a|p) + \int_{-}^{+} (a + v - D) dG(a|p) &\geq l. \end{aligned}$$

Under assumption A1, the break even constraint is binding and pins down the interest rate $r(p, v, D, c)$. The difference to the binary payoff model is that the interest rate depends not only on p but also on (v, D, c) . Adding the investment condition and the break-even constraint yields

$$\int_{-}^{\infty} (a + v - D) dG(a|p) \geq l + \int_{-}^{\infty} (a + c - D) dG(a|p).$$

Using $l = x - c$, we rearrange the terms to get the investment region

$$L(p, v) = v \int_{-}^{\infty} dG(a|p) + \int_{-}^{\infty} (a + v - D) dG(a|p) + c \int_0^{\infty} dG(a|p) - x \quad (22)$$

Shareholder value in the investment region is

$$\begin{aligned} E_1[y|p, v] &= E_1[y|p, v] - E_1[y|p, v] - E_1[y|p, v] \\ &= \int_{-}^{\infty} (a + c - D) dG(a|p) + L(p, v). \end{aligned}$$

Expected shareholder value at time 0 and at time 1 are

$$\begin{aligned} E_1[y|p, v] &= \int_{-}^{\infty} (a + c - D) dG(a|p) + L(p, v) 1_{(\cdot) \in \circ} \\ E_0[y] &= \int_{-}^{\infty} (a + c - D) dF_0(a) + \iint_{\circ} L(p, v) dF(p, v) \end{aligned}$$

Cash against equity

Suppose the government purchases equity share α in exchange for cash m . All equations to the debt overhang analysis still apply except $c = c_0 + m$. Hence, expected shareholder value at time 0 is

$$E_0[y(m)] = \int_{-}^{\infty} (a + c_0 + m - D) dF_0(a) + \iint_{(\cdot)} L(p, v) dF(p, v)$$

with

$$L(p, v) \equiv v \int_{-}^{\infty} dG(a|p) + \int_{-}^{\infty} (a + v - D) dG(a|p) + (c_0 + m) \int_0^{\infty} dG(a|p) - x.$$

The equity holder participation constraint is

$$E_0[y(m)] - E_0[y(0)] \geq \alpha E_0[y(m)]$$

and the cost to the government is

$$\Psi(m) = m - \alpha E_0[y(m)].$$

Because the investment domain only depends on m , the government chooses equity share α to ensure that the equity holder participation constraint is binding. Hence, we have

$$\Psi(m) = m - (E_0[y(m)] - E_0[y(0)])$$

with

$$\begin{aligned} E_0[y(m)] - E_0[y(0)] &= m \int_{-\infty}^0 dF_0(a) + \int_{-\infty}^0 (a + m + c_0 - D) dF_0(a) \\ &\quad + \int \int_{(\cdot)} L(p, v) dF(p, v) - \int \int_{\circ} L(p, v) dF(p, v). \end{aligned}$$

Asset buy back

The cost of asset buy backs depends on the structure of debt covenants. Consistent with the binary asset distribution case, we define efficient debt covenants for the continuous asset distribution case as follows. We assume banks can sell assets to the government with bank payoff $a - \beta(a)$ and government payoff $\beta(a)$. Debt covenants are restrictions on the function $\beta(a)$. We assume covenants are efficient if and only if for any asset distribution F , debt holders receive at least the expected payoff they would receive without asset buy backs:

$$\beta(a) \text{ acceptable iff } \int_0^{\infty} \min(a + c - \beta(a), D) dF(a) \geq \int_0^{\infty} \min(a + c, D) dF(a) \geq \text{ for all } F$$

Suppose there exists an asset payoff $\hat{a} < D - c$ such that $\beta(\hat{a}) > 0$. Then choose the distribution $f(\hat{a}) = 1$. Note that $\hat{a} + c - \beta(\hat{a}) < \hat{a} + c$ which violates the condition. Similarly, if there is an $\hat{a} > D - c$ with $\hat{a} + c - \beta(\hat{a}) < D$, the condition is violated. So the solution is that β must satisfy:

$$\begin{aligned} \beta(a) &= 0 \text{ for all } a \leq D - c \\ \beta(a) &\leq a + c - D \text{ for all } a > D - c \end{aligned}$$

In words, efficient covenants ensure that senior debt holders have priority over asset purchasers for any asset distribution F . So bank payoff are $\tilde{a} = a - \beta(a)$ with $\beta(a) = 0$ for all $a \leq D - c$ and $\beta(a) \leq a + c - D$ for $a > D - c$. The investment condition for asset buy backs is:

$$\begin{aligned} \int_{+\infty}^{-\infty} (a + v - D - rl) dG(a|p) + \int_{-\infty}^{-\infty} (\tilde{a} + v - D - rl) dG(a|p) &> \int_{-\infty}^{-\infty} (\tilde{a} + c - D) dG(a|p) \\ \int_{+\infty}^{-\infty} (a + v - D - rl) dG(a|p) + \int_{-\infty}^{-\infty} (v - rl - c) dG(a|p) &> 0 \iff v - rl - c > 0 \end{aligned}$$

The participation constraint for junior creditors is:

$$rl \int_{+\infty}^{-\infty} dG(a|p) + \int_{-\infty}^{+\infty} (a + v - D) dG(a|p) \geq l$$

Note that the investment condition is the same as with cash against equity and independent of \tilde{a} . Hence, the investment region is the same (with $c = c_0 + m$). The cost to the government is

$$\Psi = m - E_0[\beta(a)].$$

Because the investment region only depends on cash c , the government chooses $\beta(a)$ to ensure that the participation constraint is binding. Note that $\beta(a)$ comes entirely from shareholder payoffs because senior debt holders are protected by covenants. As a result, the expected proceeds from asset buy backs are

$$E_0[\beta(a)] = E_0[y(m)] - E_0[y].$$

Note that the expected cost to the government is the same as under cash against equity.

Debt guarantee

Under the debt guarantee, the proceeds from issuing debt at time 1 are

$$c = c_0 + (1 - \phi)S.$$

The investment condition is

$$\int_{+}^{+} (a + v - D - rl - S) dG(a|p) \geq \int_{+}^{+} (a + c - D - S) dG(a|p).$$

Hence, the investment condition is again $v - rl > c$. It is important that the government is junior to time 1 creditors, otherwise the government creates its own debt overhang. Under this assumption, the break-even constraint for junior creditors is

$$rl \int_{+}^{+} dG(a|p) + \int_{-}^{+} (a + v - D) dG(a|p) \geq l$$

Note that this means the interest rate is the same as in the cash against equity case. In particular it does not depend on the face value of debt issuance S . As a result, the investment region is the same as in cash against equity.

Regarding the costs of the program, there are two alternative interpretations. The first one is that the bank borrows directly from government. Then government recovers

$$\int_{(-) \in (-)} \int_{+}^{+} \min(a + v - D - rl, S) dG(a|p) + \int_{(-) \in (-)} \int_{-}^{-} \min(a + c - D, S) dG(a|p)$$

which is equivalent to $E_0[y(m, 0)] - E_0[y(m, S)]$. The binding participation constraint implies that

$$E_0[y(m, S)] = E_0[y]$$

so the cost to the government is

$$\Psi = (1 - \phi)S - (E_0[y(m, 0)] - E_0[y]) = m - (E_0[y(m)] - E_0[y]).$$

which is the same costs as for the other interventions. An alternative interpretation is that the government covers losses ex-post. This yields the same calculation because the government gets ϕS up-front and then pays S minus the recovery in good states which is the same as above because $E_0[y(m, 0)] - E_0[y(m, S)]$.

Proof of Theorem 3

We first analyze the asset buy back program at time 1. To prove the theorem, we must show equivalence along four dimensions: (i) the NIP constraint, (ii) the upper schedule, (iii) the lower schedule, and (iv) the cost function.

Upon participation and investment, equity value is

$$E_1[y(z, p) | p, v, i = 1] = p(N + c_0 - z) + L(p, v) + p z.$$

Participation without investment yields

$$E_1[y(z, p) | p, v, i = 0] = p(N + c_0 - z + p z).$$

Now consider the three constraints:

- NIP: $E_1[y(z, p) | p, v, i = 0] < E_1[y(0, 0) | p, v, i = 0]$ or

$$p < 1.$$

- Upper schedule: $E_1[y(0, 0) | p, v, i = 1] > E_1[y(z, p) | p, v, i = 1]$ or

$$p > p^*.$$

- Lower schedule: $E_1[y(z, p) | p, v, i = 1] > E_1[y(0, 0) | p, v, i = 0]$ or

$$L_1(p, v; z, p) \equiv L(p, v) + (p^* - p)z > 0.$$

Note that banks therefore set z either to 0 or to Z . Using the notations of the debt guarantee section, the participation set is

$$\Omega_1(Z, 1 - p^*)$$

where Ω_1 is defined above in equation (16). The expected cost of the program is

$$\Psi_1(Z, p^*) = Z \int_{\Omega^g(1 - z^*)} (p^* - p) dF(p, v) = \Lambda_1(Z, 1 - p^*)$$

and the investment domain is

$$I \cup \Omega_1(Z, 1 - p^*).$$

Now if we set $S = Z$ and $p^* = 1 - \phi$, we see that the NIP constraint, the upper and lower schedules, and the cost function are the same for the asset buy back program as for the debt guarantee program. The two programs are therefore equivalent.

Proof of Theorem 4

We first analyze the cash against equity program at time 1. Upon participation and investment, equity value (including the share going to the government) is

$$E_1[y(m) | p, v, i = 1] = p(N + c_0) + L(p, v) + m$$

Participation without investment yields

$$E_1[y(m) | p, v, i = 0] = p(N + c_0 + m)$$

Now consider the three constraints

- NIP: $(1 - \alpha) E_1[y(m) | p, v, i = 0] < E_1[y(0) | p, v, i = 0]$ or:

$$(1 - \alpha) m < \alpha (N + c_0).$$

- Upper schedule: $E_1[y(0) | p, v, i = 1] > (1 - \alpha) E_1[y(m) | p, v, i = 1]$ or:

$$\alpha (p(N + c_0) + L(p, v)) > (1 - \alpha) m.$$

- Lower schedule: $(1 - \alpha) E_1[y(m) | p, v, i = 1] > E_1[y(0) | p, v, i = 0]$ or:

$$(1 - \alpha) (L(p, v) + m) > \alpha p(N + c_0).$$

We define the function

$$X(p; m, \alpha) \equiv (1 - \alpha) m - \alpha p(N + c_0)$$

We can summarize the cash against equity program by:

$$\begin{aligned} L_1(p, v; m, \alpha) &\equiv (1 - \alpha) L(p, v) + X(p; m, \alpha) \\ U_1(p, v; m, \alpha) &\equiv \alpha L(p, v) - X(p; m, \alpha) \\ NIP &: X(1; m, \alpha) < 0. \end{aligned}$$

The participation set is

$$\Omega_1(m, \alpha) = \{(p, v) \mid L_1(p, v; m, \alpha) > 0 \wedge U_1(p, v; m, \alpha) < 0\}.$$

The cost function is therefore

$$\Psi_1(m, \alpha) = \int_{\Omega_1^e} \int (m - \alpha E_1[y(m, \alpha) | p, v, i = 1]) dF(p, v).$$

We can rewrite the cost function such that

$$\Psi_1(m, \alpha) = \int_{\Omega_1^e} \int X(p; m, \alpha) dF(p, v) - \alpha \int_{\Omega_1^e} \int L(p, v) dF(p, v).$$

The following table provides a comparison of the three government interventions:

	Debt guarantee	Asset buy back	Equity injection
Participation	$\Omega_1(S, \phi)$	$\Omega_1(Z, 1 - p)$	$\Omega_1(m, \alpha)$
Investment I_1	$I \cup \Omega_1(S, \phi)$	$I \cup \Omega_1(Z, 1 - p)$	$I \cup \Omega_1(m, \alpha)$
NIP constraint	$\phi > 0$	$p < 1$	$X(1, m, \alpha) < 0$
Cost function	$\Lambda_1(S, \phi)$	$\Lambda_1(Z, 1 - p)$	$\Psi_1(m, \alpha)$

Now let us prove that the cash against equity program dominates the other two programs. Take a program S, ϕ . We are going to construct an equity program that has same welfare gains at lower cost. To get equity with same lower bound graph we need to ensure that:

$$L_1(p, v; m, \alpha) = L_1(p, v; S, \phi) \text{ for all } p, v.$$

So we must have

$$X(p; m, \alpha) = (1 - \alpha)(1 - \phi - p)S \text{ for all } p. \quad (23)$$

It is easy to see that this is indeed possible if we identify term by term: $\frac{-}{1-} = \frac{-}{+ 0-}$ and $m = (1 - \phi)S$. Therefore it is possible to implement exactly the same lower schedules. Formally, we have just shown that:

$$I_1(S, \phi) = I_1(m, \alpha).$$

Next notice that the NIP constraints are equivalent since:

$$X(1, m, \alpha) < 0 \iff \phi > 0.$$

Now consider the upper bound. Consider the lowest point on the upper schedule of the guarantee program, i.e., the intersection of $U_1(p, v; S, \phi) = 0$ with $L(p, v) = 0$. At that point, we have $\tilde{p} = 1 - \phi$ and $\tilde{v} = (x - \phi c_0) / (1 - \phi)$. But from (23), it is clear that $X(\tilde{p}; m, \alpha) = 0$, and therefore $U_1(\tilde{p}, \tilde{v}; m, \alpha) = \alpha L(\tilde{p}, \tilde{v}) - X(\tilde{p}; m, \alpha) = 0$. Therefore the upper schedule $U_1(p, v; m, \alpha) = 0$ also passes by this point. But the schedule $U_1(p, v; m, \alpha) = 0$ is downward slopping in (p, v) , so the domain of inefficient participation is smaller (see Figure 7) than in the debt guarantee case. Formally, we have just shown that:

$$\Omega_1(m, \alpha) \subset \Omega_1(S, \phi).$$

As an aside, it is also easy to see that the schedule $U_1(p, v; m, \alpha) = 0$ is above the schedule $L(p, v) = 0$ so it does not get rid completely of opportunistic participation, but it helps.

The final step is to compare the cost functions.

$$\Lambda_1(S, \phi) \equiv S \int \int_{\Omega_1^g(\cdot)} (1 - p - \phi) dF(p, v)$$

$$\Psi_1(m, \alpha) = \int \int_{\Omega_1^e(\cdot)} X(p; m, \alpha) dF(p, v) - \alpha \int \int_{\Omega_1^e(\cdot)} L(p, v) dF(p, v)$$

By definition of the participation domain, we know that $L_1(p, v; m, \alpha) > 0$. Therefore:

$$-\int \int_{\Omega_1^e(\cdot)} L(p, v) dF(p, v) < \frac{X(p; m, \alpha)}{1 - \alpha} \text{ for all } (p, v) \in \Omega_1(m, \alpha)$$

Therefore

$$\Psi_1(m, \alpha) < \frac{1}{1 - \alpha} \int \int_{\Omega_1^e(\cdot)} X(p; m, \alpha) dF(p, v) = S \int \int_{\Omega_1^e(\cdot)} (1 - \phi - p) dF(p, v)$$

Finally, since $1 - \phi - p > 0$ for all $(p, v) \in \Omega_1(m, \alpha)$, and since $\Omega_1(m, \alpha) \subset \Omega_1(S, \phi)$, we have

$$\Psi_1(m, \alpha) < \Lambda_1(S, \phi).$$

Proof of Proposition 4

Cost Function at Time 0

First we define $v_0(p)$ as

$$L(p, v_0(p)) + (1 - p)m = 0.$$

Then we define the piecewise linear function

$$\zeta(v, p) \equiv pm_{[0, v_0(p)]} + (L(p, v) + (1 - p)m)1_{[v_0(p), 1]} + m1_{[0, v_0(p)]}.$$

We rewrite the cost function of the cash program as

$$\begin{aligned} \Lambda_0(m; F) &= m - \iint \zeta(v, p) dF(p, v) \\ &= m - E[\zeta(v, p) | F]. \end{aligned}$$

The function ζ is increasing in v and in p , therefore FOSD of \tilde{F} on F , implies that $E[\zeta(v, p) | \tilde{F}] > E[\zeta(v, p) | F]$. Hence, $\Lambda_0(m; \tilde{F}) < \Lambda_0(m; F)$.

Time 1 programs can dominate

First we choose a time 0 program with cash m and optimal cost $\Lambda_0(m)$. Then we choose a time 1 debt guarantee program with $\phi = 0$ and $S = m$ to get same investment set. The cost of the debt guarantee program is

$$\begin{aligned} \Lambda_1(m, 0) &= m \iint (1 - p) dF(p, v) \\ \Lambda_0(m) &= m \iint (1 - p) dF(p, v) - \iint L(p, v) dF(p, v) \end{aligned}$$

Where $T = [0, V] \times [0, 1]$. Clearly, we have $\Lambda_1(m, 0) < \Lambda_0(m)$ when $\iint dF(p, v)$ is small

enough. Just because of the fact that time 1 programs do not give provide cash to banks that do not invest. This is *a fortiori* true for equity injection since they dominate at time 1.

Time 0 programs can dominate

We consider a large government program such that all firms invest. Then it must be that $Zp = x - c_0$ and $p = 1$. We then choose $m = x - c_0$. Then $I(m) = I^* = \Omega(Z, p)$. Now

$$\begin{aligned} \Lambda_1(Z, 0) &> \Lambda_0(m) \\ &\iff \\ (x - c_0) \iint (1 - p) dF(p, v) &> (x - c_0) \iint (1 - p) dF(p, v) - \iint L(p, v) dF(p, v). \end{aligned}$$

Now clearly when $\Pr(I^*) \rightarrow 1$, then $\Pr(T \setminus I^*) \rightarrow 0$, so $(x - c_0) \int \int_{\setminus *} (1 - p) dF(p, v) \rightarrow 0$.

Over I^* , we know that $v > x$, hence $-L(p, v) < (1 - p)(x - c_0)$, therefore

$$-\int \int_{* \setminus o} L(p, v) dF(p, v) < (x - c_0) \int \int_{* \setminus o} (1 - p) dF(p, v) \leq (x - c_0) \int \int_* (1 - p) dF(p, v).$$

Proof of Proposition 6

First note that the optimization problem from the equity holders perspective remains unchanged because the investment and participation decision only depend on total debt D . Now consider the expected cost of deposit insurance. Note that the time 0 expected value of deposits is Δ because $\Delta \leq \underline{A} + c_0$. Hence, the cost of government intervention is unchanged and therefore the cost and benefits of both time 0 and time 1 programs are unchanged.

Proof of Proposition 7

We distinguish two cases depending on the recovery rate on deposits in the low payoff state.

Time 0 Programs

Full transfer: $\underline{A} + v < \Delta$

The expected values of deposits at time 1 and time 0 are

$$\begin{aligned} E_1[y^\Delta(m) | p, v] &= p\Delta + (1 - p)(\underline{A} + c_0 + m) \text{ if } (p, v) \in T \setminus I_0(m) \\ &= p\Delta + (1 - p)(\underline{A} + v) \text{ if } (p, v) \in I_0(m) \\ E_0[y^\Delta(m)] &= \bar{p}\Delta + (1 - \bar{p})(\underline{A} + c_0 + m) + \int \int_{o(\cdot)} (1 - p)(v - c_0 - m) dF(p, v). \end{aligned}$$

The expected cost of deposit insurance at time 0 is

$$\begin{aligned} \Psi_0(m) &= \Delta - E_0[y^\Delta(m)] \\ &= (1 - \bar{p})(\Delta - \underline{A} - c_0 - m) - \int \int_{o(\cdot)} (1 - p)(v - c_0 - m) dF(p, v) \end{aligned}$$

The change in the expected cost of deposit insurance is

$$\begin{aligned} \Lambda_0(m) &= \Psi_0(m) - \Psi_0(0) \\ &= -(1 - \bar{p})m + m \int \int_{o(\cdot)} (1 - p) dF(p, v) - \int \int_{o(\cdot) \setminus o} (1 - p)(v - c_0) dF(p, v). \end{aligned}$$

The net cost of government intervention is

$$\Lambda_0(m) + \Lambda_0(m) = - \int_{o(\cdot) \setminus \circ} \int_{\circ} (v - c_0) dF(p, v).$$

Note that this term is negative because the benefits of incremental investments accrue to the government.

Partial Transfer: $\underline{A} + c_0 < \Delta < \underline{A} + v$

The expected values of deposits at time 1 and time 0 are

$$\begin{aligned} E_1 [y^\Delta(m) | p, v] &= p\Delta + (1-p) \max(\Delta, \underline{A} + c_0 + m) \text{ if } (p, v) \in T \setminus I_0(m) \\ &= \Delta \text{ if } (p, v) \in I_0(m) \\ E_0 [y^\Delta(m)] &= \Delta - \int_{\setminus o(\cdot)} \int_{\circ} (1-p) (\Delta - \max(\Delta, \underline{A} + c_0 + m)) dF(p, v) \end{aligned}$$

The expected cost of deposit insurance is

$$\Psi_0(m) = \int_{\setminus o(\cdot)} \int_{\circ} (1-p) (\Delta - \max(\Delta, \underline{A} + c_0 + m)) dF(p, v).$$

The change in the expected cost of deposit insurance

$$\Lambda_0(m) = \int_{\setminus o(\cdot)} \int_{\circ} (1-p) (\Delta - \max(\Delta, \underline{A} + c_0 + m)) dF(p, v) - \int_{\setminus \circ} \int_{\circ} (1-p) (\Delta - \underline{A} - c_0) dF(p, v).$$

Note that when $\Delta \rightarrow (\underline{A} + c_0)$, then $\Lambda_0(m) \rightarrow 0$. This means the expected change in the cost of deposit insurance goes to zero as deposits become safe. Also note that when $\Delta \rightarrow (\underline{A} + v)$, then

$$\Lambda_0(m) \rightarrow -(1-\bar{p})m + m \int_{o(\cdot)} \int_{\circ} (1-p) dF(p, v) - \int_{o(\cdot) \setminus \circ} \int_{\circ} (1-p) (v - c_0) dF(p, v)$$

which is the change in expected cost of deposit insurance in the full transfer case. The government cost is $\Lambda_0(m) + \Lambda_0(m)$. The results apply to all programs because all programs have the same cost function at time 0.

Asset buy backs at time 1

Full Transfer: $\underline{A} + v < \Delta$

The expected values of deposits at time 1 and time 0 are

$$\begin{aligned} E_1 [y^\Delta(Z, p) | p, v] &= p\Delta + (1-p) (\underline{A} + c_0) \text{ if } (p, v) \in T \setminus (I \cup \Omega_1(Z, 1-p)) \\ &= p\Delta + (1-p) (\underline{A} + v) \text{ if } (p, v) \in I \cup \Omega_1(Z, 1-p) \\ E_0 [y^\Delta(Z, p)] &= \bar{p}\Delta + (1-\bar{p}) (\underline{A} + c_0) + \int_{\circ \cup \Omega_1^q(1-z)} \int_{\circ} (1-p) (v - c_0) dF(p, v) \end{aligned}$$

The expected cost of deposit insurance is

$$\Psi_0 (Z, p) = (1 - \bar{p}) (\Delta - \underline{A} - c_0) - \int_{\circ \cup \Omega_1^g(1-p-z)} \int (1-p)(v - c_0) dF(p, v)$$

The change in the cost of deposit insurance is

$$\Lambda_0 (Z, p) = - \int_{\Omega_1^g(1-p-z)} \int (1-p)(v - c_0) dF(p, v)$$

Expected government cost is

$$\begin{aligned} \Psi_1 (Z, p) &= Z \int_{\Omega_1^g(1-p-z)} \int (p - \bar{p}) dF(p, v) \\ &= \Lambda(Z, 1-p) - \int_{\Omega_1^g(1-p-z)} \int (1-p)(v - c_0) dF(p, v). \end{aligned}$$

Partial Transfer: $\underline{A} + c_0 < \Delta < \underline{A} + v$

The expected values of deposits at time 1 and time 0 are

$$\begin{aligned} E_1 [y^\Delta (Z, p) | p, v] &= p\Delta + (1-p)(\underline{A} + c_0) \text{ if } (p, v) \in T \setminus (I \cup \Omega_1(Z, 1-p)) \\ &= \Delta \text{ if } (p, v) \in I \cup \Omega_1(Z, 1-p) \\ E_0 [y^\Delta (Z, p)] &= \Delta - \int_{\setminus (\circ \cup \Omega_1^g(1-p-z))} \int (1-p)(\Delta - \underline{A} - c_0) dF(p, v) \end{aligned}$$

The expected cost of government insurance is

$$\Psi_0 (Z, p) = \int_{\setminus (\circ \cup \Omega_1^g(1-p-z))} \int (1-p)(\Delta - \underline{A} - c_0) dF(p, v).$$

The change in expected cost of deposit insurance is

$$\Lambda_0 (Z, p) = - \int_{\Omega_1^g(1-p-z)} \int (1-p)(\Delta - \underline{A} - c_0) dF(p, v).$$

Note that when $\Delta \rightarrow (\underline{A} + c_0)$, then $\Lambda_0 (Z, p) \rightarrow 0$. Also note that when $\Delta \rightarrow (\underline{A} + v)$, then

$$\Lambda_0 (Z, p) \rightarrow - \int_{\Omega_1^g(1-p-z)} \int (1-p)(v - c_0) dF(p, v).$$

Total government cost is

$$\begin{aligned}\Psi_1(Z, p) &= Z \int_{\Omega_1^g(1-z)} \int (p - p) dF(p, v) \\ &= \Lambda(Z, 1 - p) - \int_{\Omega_1^g(1-z)} \int (1 - p)(\Delta - \underline{A} - c_0) dF(p, v).\end{aligned}$$

The results also apply to debt guarantees at time 1 because asset buy backs and debt guarantees have the same cost function at time 1.

Cash against equity at time 1

Note that we can compute the expected cost of time 1 cash against equity similarly to the time 1 asset buy back program. The only difference is the participation region for cash against equity $\Omega(m, \alpha)$ and the participation region for asset buy back $\Omega_1(Z, 1 - p)$. It turns out that the change in the expected cost of deposit insurance $\Lambda_0(m)$ is equivalent under both programs because both in the full and partial transfer case the difference in the participation region cancels out when computing the difference in expected cost of deposit insurance. It follows that the relative ranking of programs is unchanged.

Proof of Proposition 8

To illustrate the logic, we compare the debt guarantee at time 0 with the optional debt guarantee at time 0. Participation is decided at time 0. Banks give an equity share α in exchange for the right (not the obligation) to use the debt guarantee program (S, ϕ) at time 1. The increase in shareholder value is

$$\begin{aligned}E_0[y(\Gamma)] - E_0[y] &= \int_{\Omega_1^g(\cdot)} \int L_1(p, v; S, \phi) dF(p, v) - \int_{\Omega} \int L(p, v) dF(p, v) \\ &= S \int_{\Omega_1^g(\cdot)} \int (1 - \phi - p) dF(p, v) + \int_{\Omega_1^g(\cdot) \setminus \Omega} \int L(p, v) dF(p, v) \\ &= \Lambda_1(S, \phi) + \int_{\Omega_1^g(\cdot) \setminus \Omega} \int L(p, v) dF(p, v)\end{aligned}$$

If the government asks for equity in exchange at time 0, then the net cost to the government is

$$\tilde{\Lambda}_0(S, \phi) = - \int_{\Omega_1^g(\cdot) \setminus \Omega} \int L(p, v) dF(p, v).$$

We compare the cost to the government with:

$$\Lambda_0(m) = m \int_{\Omega \setminus \Omega_1^g(\cdot)} \int (1 - p) dF(p, v) - \int_{\Omega \setminus \Omega_1^g(\cdot)} \int L(p, v) dF(p, v).$$

Where $T = [0, V] \times [0, 1]$. It is clear that with $s = m$, the investment domains are the same, and the cost saving is

$$\Lambda_0(s) - \tilde{\Lambda}_0(S, \phi) = m \int \int_{\setminus ()} (1-p) dF(p, v) - \int \int_{() \setminus \circ} L(p, v) dF(p, v) + \int \int_{\frac{g}{1}() \setminus \circ} L(p, v) dF(p, v)$$

So it is clear that the ex-ante optional program strictly dominates in all cases. First, one can always set $\phi = 0^+$ and $S = m$ in which case $I_1(S, \phi) = I(m)$ and the cost reduction is

$$m \int \int_{\setminus ()} (1-p) dF(p, v)$$

which corresponds to idle cash wasted on banks that do not make new investment.

Proof of Proposition 9

We now show that pure equity dominates over combination of equity with other programs. Let m be cash injection, i.e., sum of m' from equity and pZ from asset buy-back. We define the function

$$X(p) \equiv (1 - \alpha)(m - pZ) - \alpha p(N + c_0)$$

The three constraints are:

$$\begin{aligned} NIP & : X(1) < 0 \\ L & \equiv (1 - \alpha)L(p, v) + X(p) \\ U & \equiv \alpha L(p, v) - X(p) \end{aligned}$$

The participation set is

$$\Omega = \{(p, v) \mid L > 0 \wedge U < 0\}$$

The cost function is

$$\Psi = \iint_{\Omega} X(p) dF(p, v) - \alpha \iint_{\Omega} L(p, v) dF(p, v) \quad (24)$$

Now take any program. To get the same investment set, we need the same lower bound and therefore the same function $X(p)$. But then we now from (24) that the cost function is the same. Also we know that the NIP constraint is $X(1) < 0$, so it is also the same. Thus, all that matters is the participation domain Ω . So we need only to look at the upper bound U . We want to exclude as many banks as possible, so we want U to be as high as possible. The way to do so is obviously to have α as high as possible. But of course we must keep the function $X/(1 - \alpha)$ constant. Therefore we must keep $Z + \frac{1}{1-\alpha}(N + c_0)$ constant. As α goes up, Z must go down. Therefore we want to set $Z = 0$. Therefore asset buy back cannot improve the equity program. The same proof also applies to debt guarantees.

Proof of Proposition 10

In the good state, the residual payoffs conditional on investment are

$$N + c_0 + m + \frac{L(p, v) + (1 - p)m}{p}$$

The loan is repaid first. Then shareholders receive

$$\begin{aligned} y &= \max \left(N + c_0 + \frac{L(p, v) + (1 - p)m}{p} - hm, 0 \right) \text{ if } i = 1 \text{ and } a = A \\ y &= \max(N + c_0 - hm, 0) \text{ if } i = 0 \text{ and } a = A. \end{aligned}$$

As soon as $y > N + c_0$, the warrants are in the money and the number of shares jumps to $1 + \frac{1}{\varepsilon} = \frac{1}{\varepsilon}$. So the old shareholders get only a fraction ε of the value beyond $N + c_0$. Their payoff function is therefore:

$$f(y) = \min(y, N + c_0) + \varepsilon \max(y - N - c_0, 0).$$

So old shareholders are full residual claimants up to the face value of old assets $N + c_0$ and ε residual claimants beyond. Now let us think about their decisions at time 1. As usual only the payoffs in the non default state matter. If they do not invest they get $N + c_0$. If they invest, they receive more if and only if $L(p, v) + (1 - p)m > phm$. The lower participation constraint is therefore

$$L(p, v) + (1 - (1 + h)p)m > 0.$$

It converges to $L(p, v) + (1 - p)m$ if $h \rightarrow 0$. We can compare this to the equity injection schedule $L_1(p, v; m, \alpha)$, we can identify the same cash injection m , and the dilution factor

$$\alpha = \frac{m(1 + h)}{N + c_0 + m(1 + h)}.$$

If we compare to debt guarantee $L_1(p, v; S, \phi) = L(p, v) + (1 - \phi - p)S$. Then

$$m = (1 - \phi)S \text{ and } h = \frac{\phi}{1 - \phi}.$$

Next consider the upper schedule. Investing alone gets $N + c_0 + L(p, v)/p$ so they opt in if and only if $L(p, v) > \varepsilon(L(p, v) + (1 - (1 + h)p)m)$ and therefore

$$U = L(p, v) - m\varepsilon \frac{1 - (1 + h)p}{1 - \varepsilon}.$$

The upper bound converges to $L(p, v)$ when $\varepsilon \rightarrow 0$. The NIP constraint is simply

$$h > 0.$$

Finally, the cost of the program is small because the government gets all the upside value of the new projects. The expected payments to the old shareholders converge to $p(N + c_0)$. So the government receives expected value $L(p, v) + m$ by paying m at time 1. The total cost is therefore:

$$-\int \int_{(\Gamma) \setminus \circ} L(p, v) dF(p, v)$$

The cost is positive because $L(p, v) < 0$ for all $(p, v) \in I(m) \setminus I$.

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Fig 1: Information & Technology

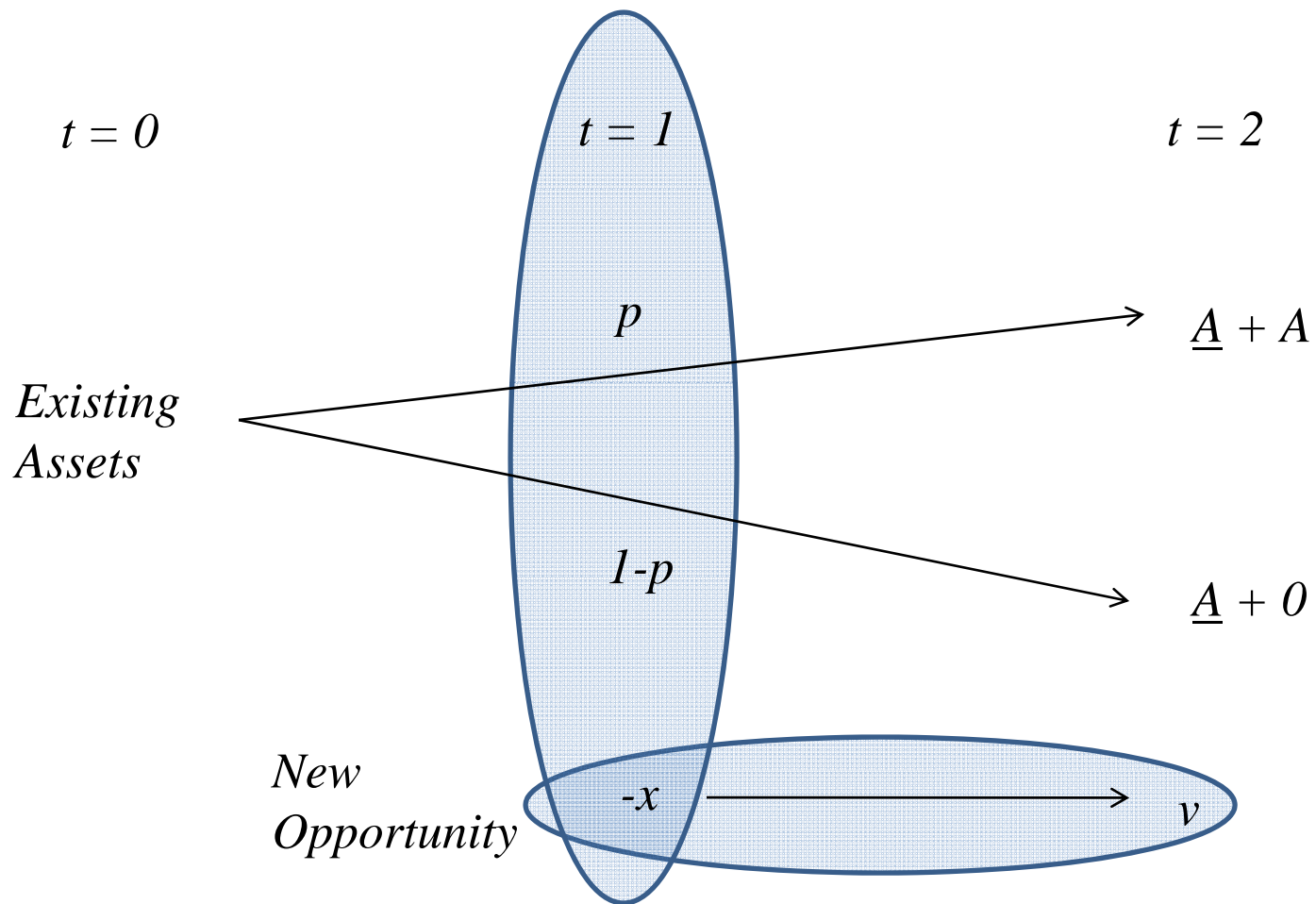


Fig 2: Payoffs

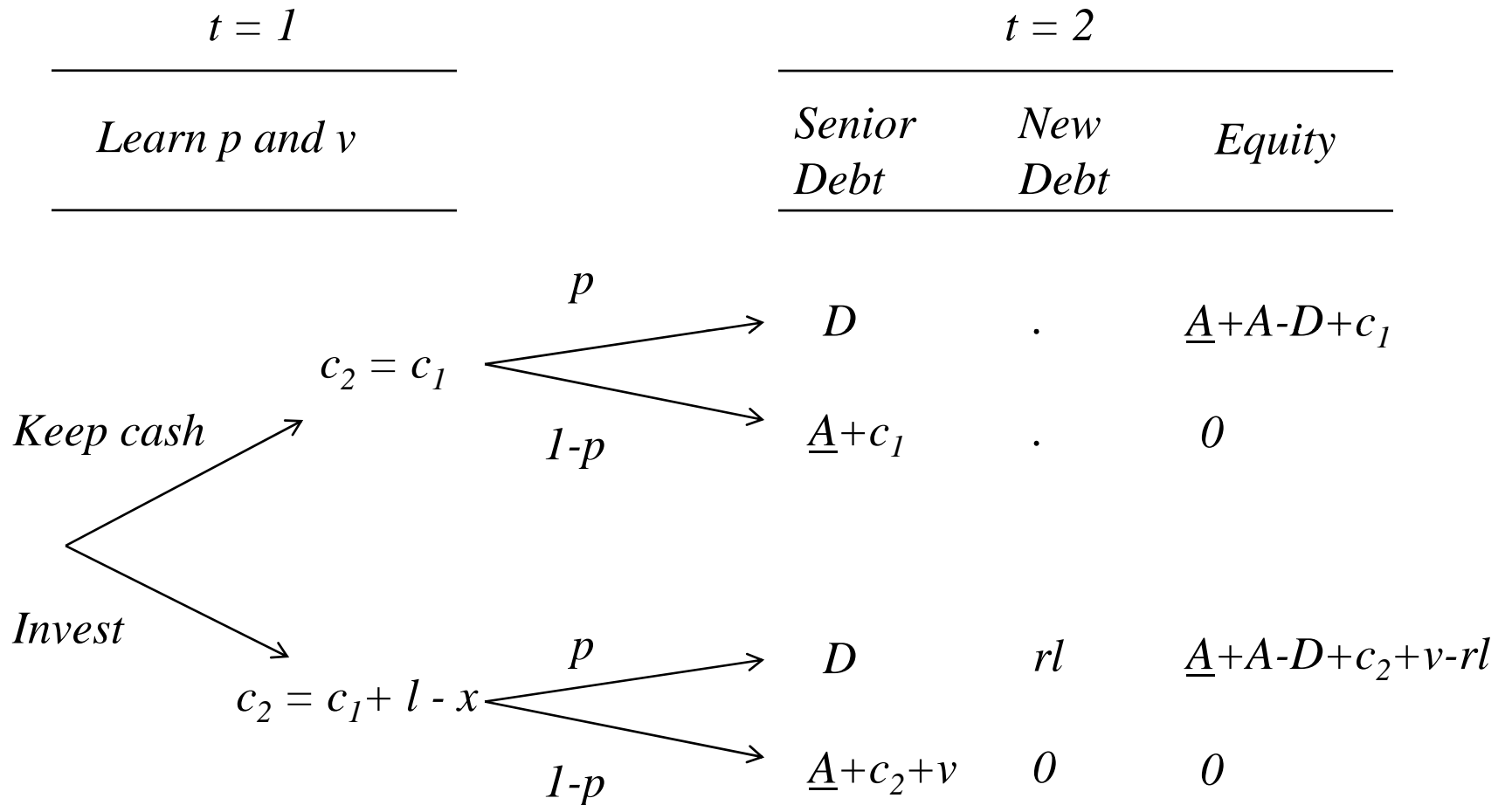


Fig 3: First Best

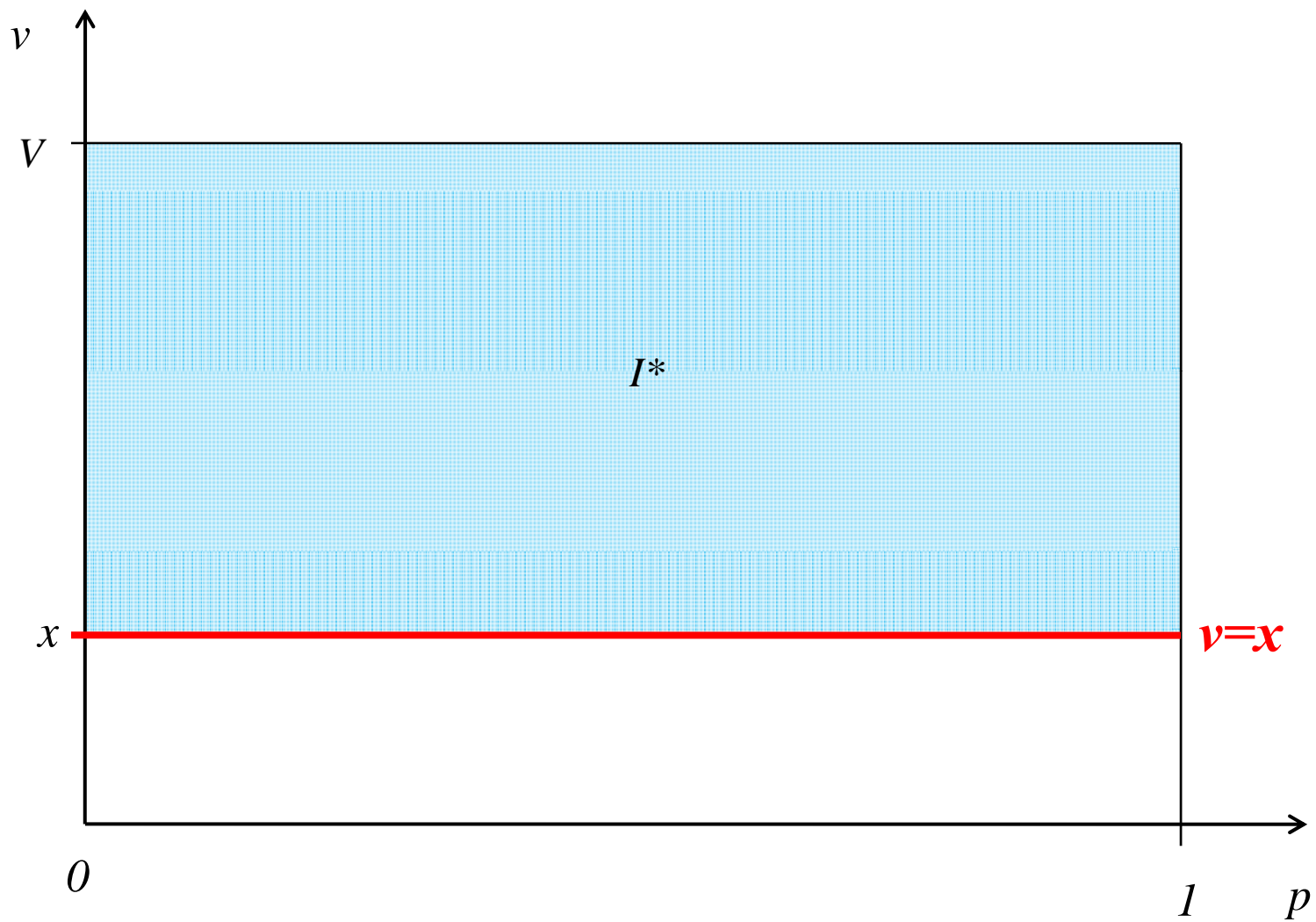


Fig 4: Debt Overhang

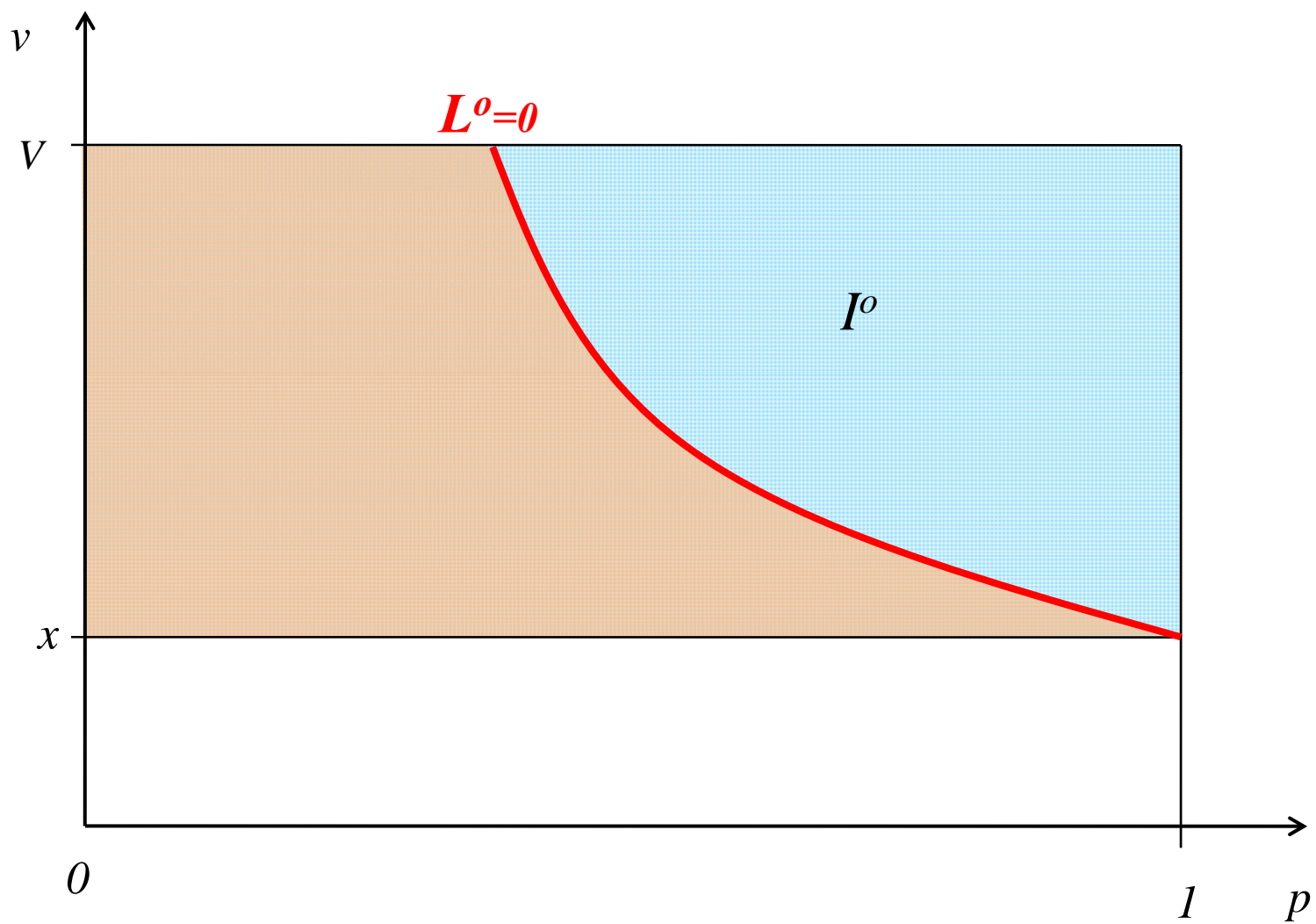


Fig 5: Cash at time 0

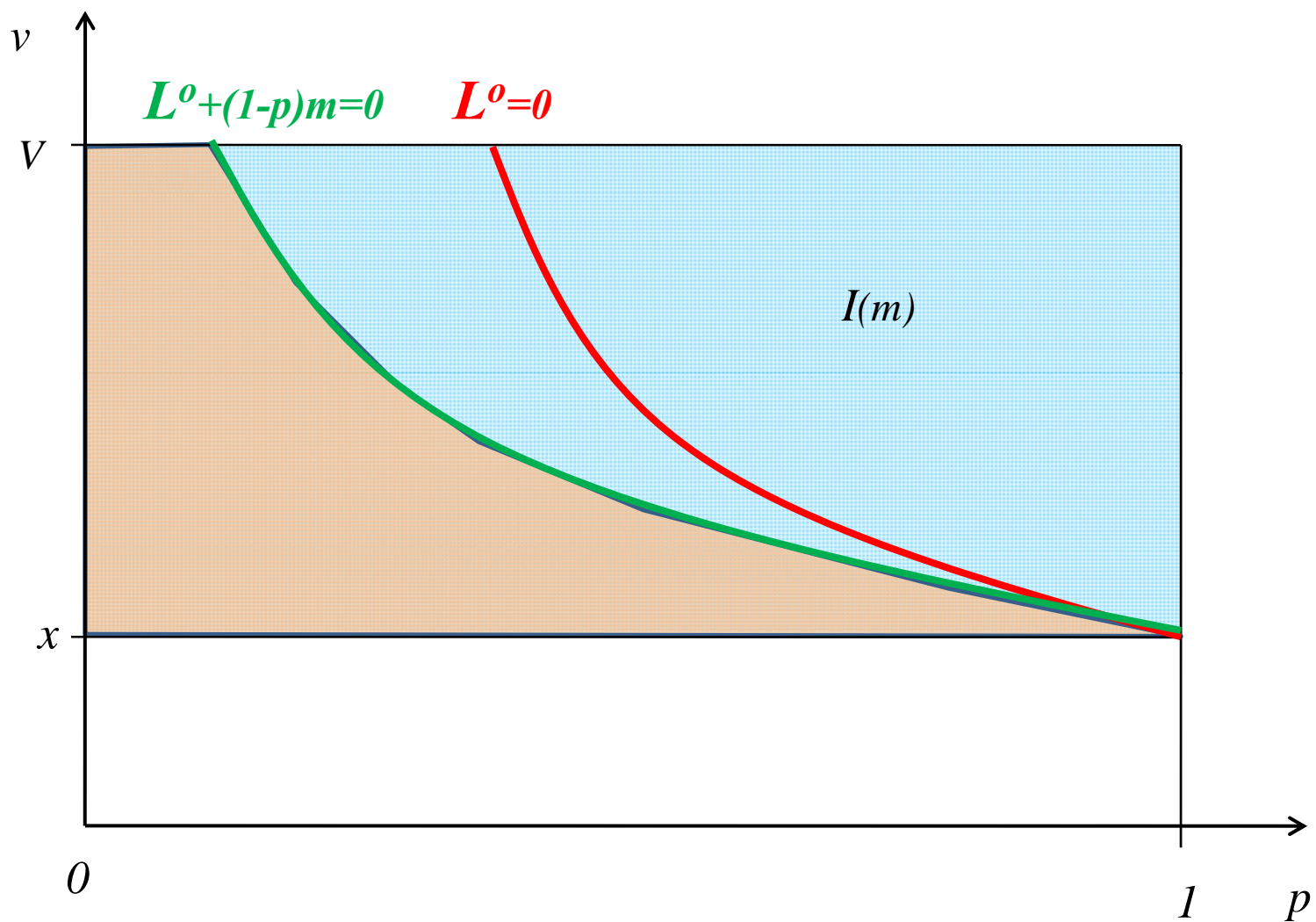


Fig 6: Debt Guarantee at time 1

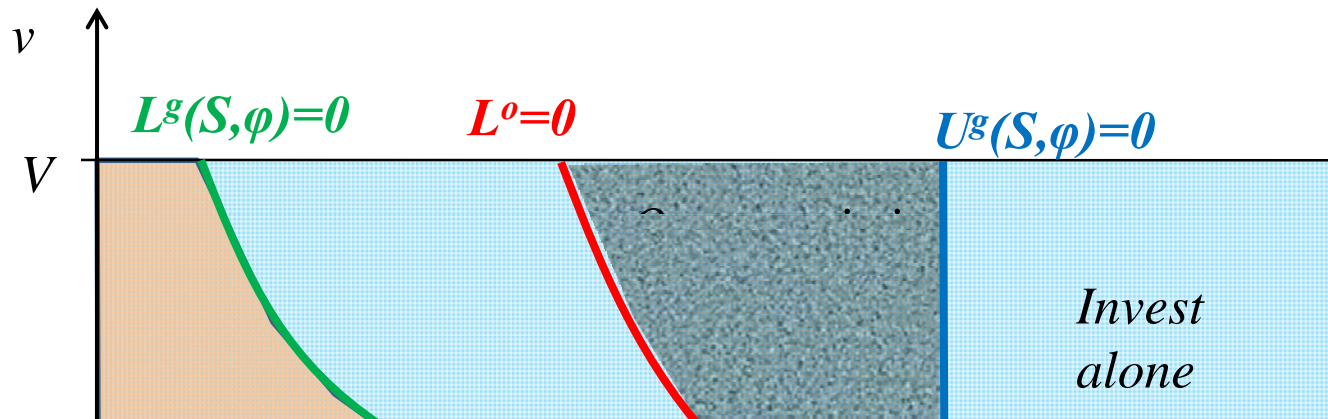


Figure 7: Equity injection at time 1

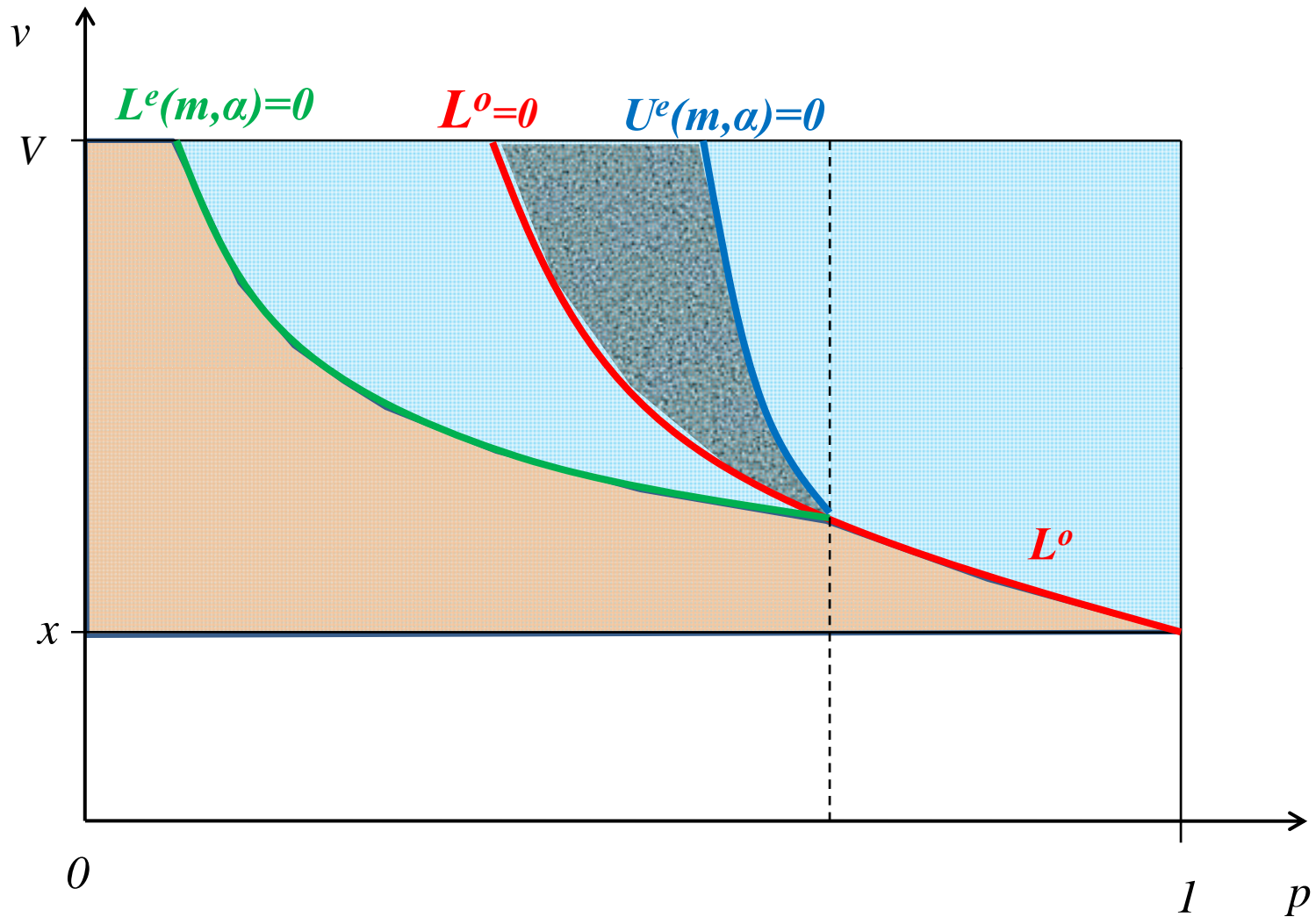


Figure 8: Efficient Mechanism

